

Unit 7

Equilibrium

7.1 Introduction to Equilibrium

7.2 Direction of Reversible Reactions

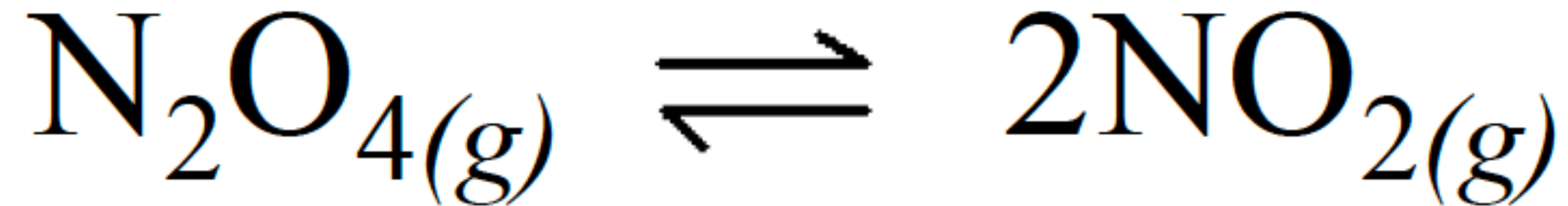
7.3 Reaction Quotient & Equilibrium Constant

- Establishing Equilibrium
- Equilibrium Constants (K_c and K_p)
- Reaction Quotients (Q_c and Q_p)

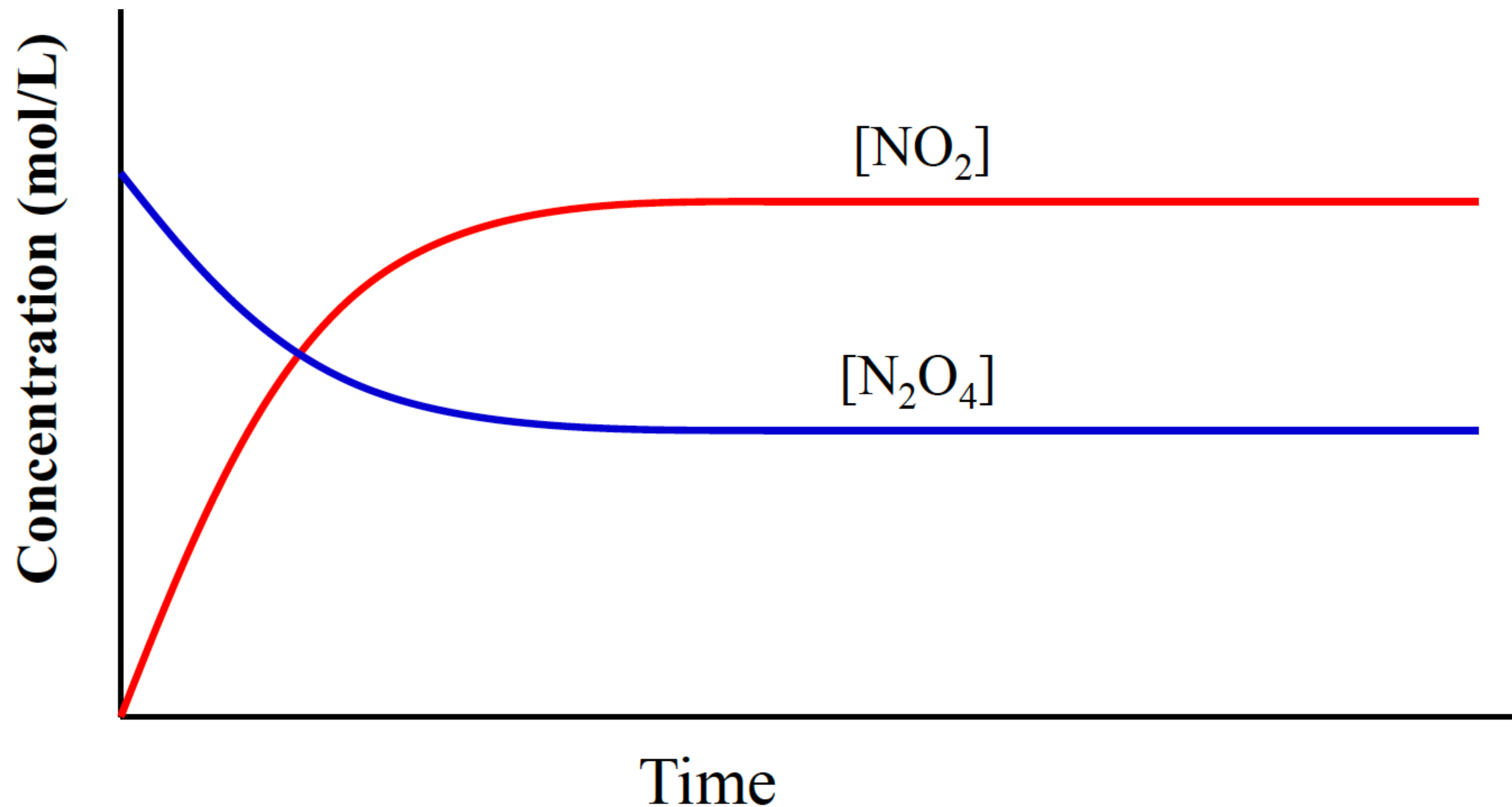
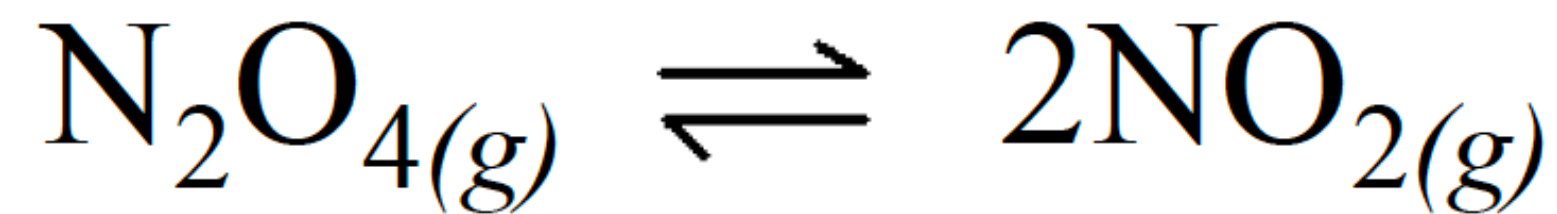
Dynamic Equilibrium

Most reactions do not go to completion.

- Here, all of the reactants **do not** get used up.
- The system reaches a dynamic state where reactants are continually turning into products, and products are continually turning back into reactants.

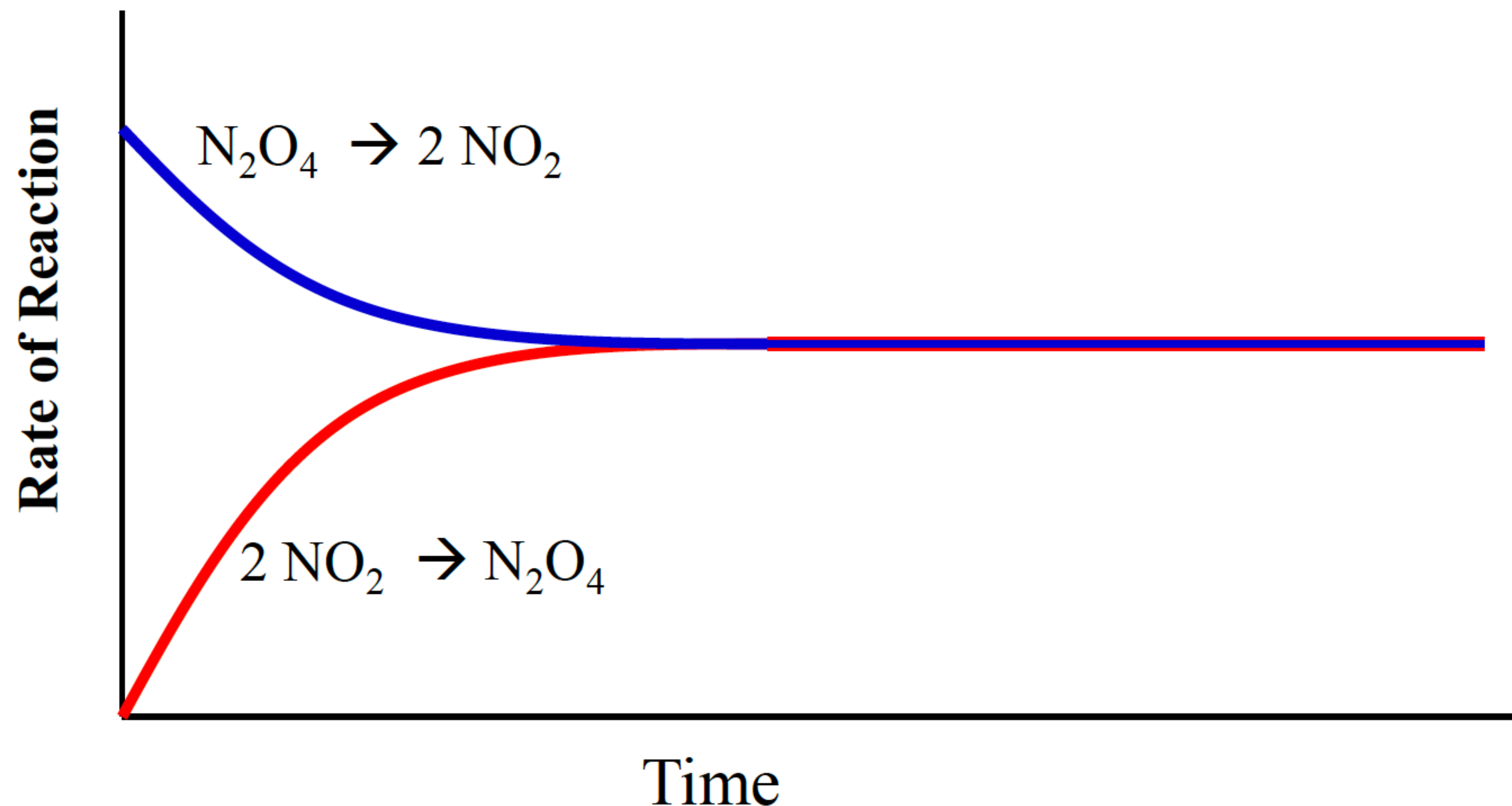
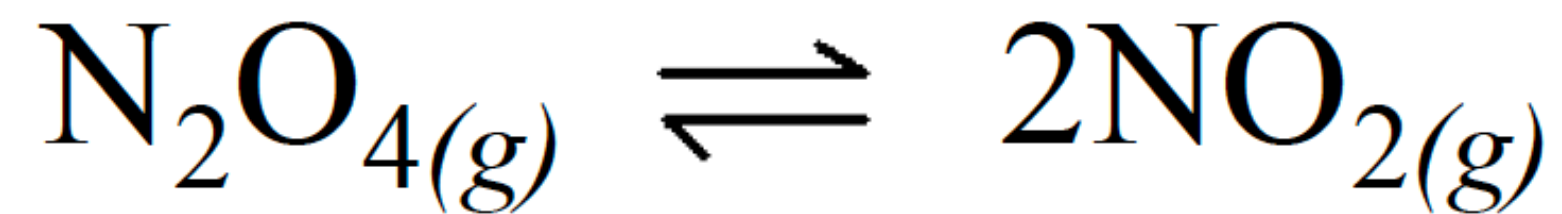


Dynamic Equilibrium



In this example, the system *initially contains only reactants, N_2O_4 , and eventually establishes equilibrium.*

Dynamic Equilibrium



In this example, the system *initially contains only reactants, N_2O_4 , and eventually establishes equilibrium.*

Establishing Chemical Equilibrium

- When the rate of the **forward reaction** is greater than the rate of the reverse reaction, there is a net conversion of reactants into products.
- The reversible reaction is **proceeding to the right**.
- When the rate of the **reverse reaction** is greater than the the rate of the forward reaction, there is a net conversion of products into reactants.
- The reversible reaction is **proceeding to the left**.

Once Equilibrium is Established

- **No observable changes occur even though...**
 - Forward and reverse reactions continue to take place.
 - The rate of the forward reaction **EQUALS** the rate of the reverse reaction.
- **Concentrations and/or partial pressures of all species remain constant, yet they will rarely be equal to one another.**

Maintaining Equilibrium

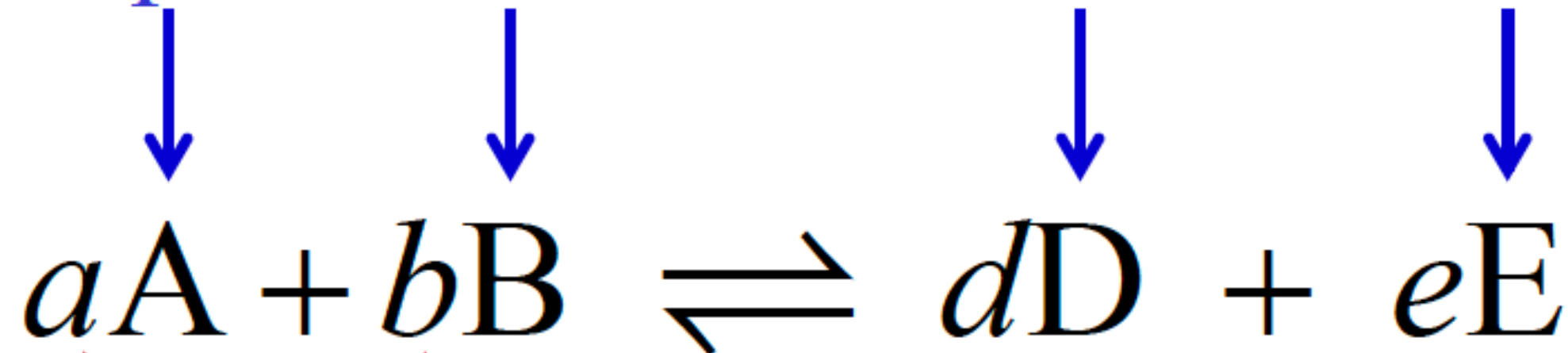
Closed System

Volume Remains Constant

Temperature Remains Constant

The Equilibrium Constant (K_{eq})

Species involved in the reaction



stoichiometric coefficients

square brackets represent concentration in [mol/L]

concentration constant

$$K_c = \frac{[D]^d [E]^e}{[A]^a [B]^b}$$

Units for Concentration
mol/L = M

Example: Equilibrium Expression (K_c)

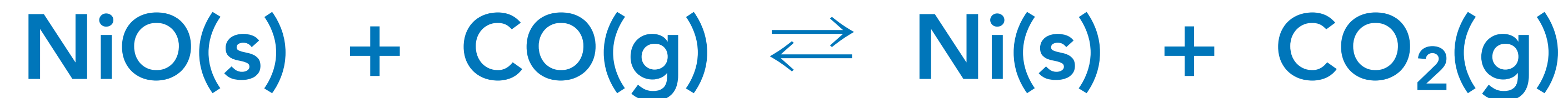
Write the equilibrium expression, K_c , for:



$$K_c = \frac{[\text{NO}]^2}{[\text{N}_2][\text{O}_2]}$$

Example: Equilibrium Expression (K_c)

Write the equilibrium expression, K_c , for:

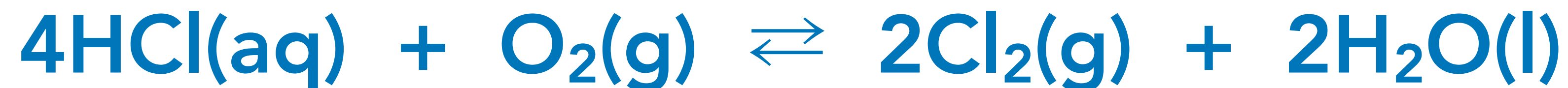


$$K_c = \frac{[\text{CO}_2]}{[\text{CO}]}$$

- $[\text{NiO}]$ has not changed.
- Concentration is measured in mol/L.
- Both pieces have the same density, so both contain the same number of particles per unit volume.

Example: Equilibrium Expression (K_c)

Write the equilibrium expression, K_c , for:

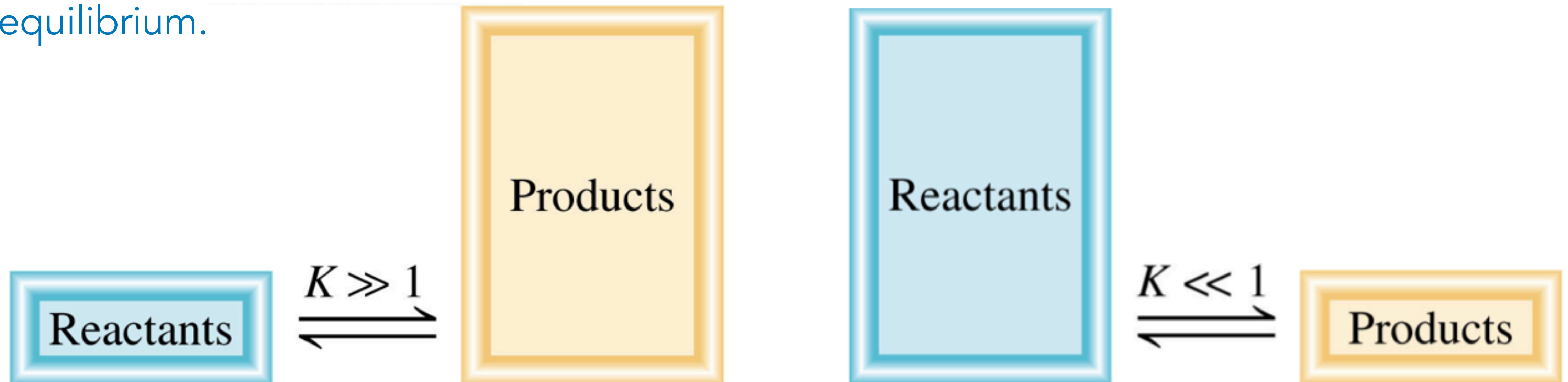


$$K_c = \frac{[\text{Cl}_2]^2}{[\text{HCl}]^4 [\text{O}_2]}$$

- Adding or taking away small amounts of water in a reaction that takes place in an aqueous solution does not affect the overall concentration of H_2O

Details About the Equilibrium Constant, K

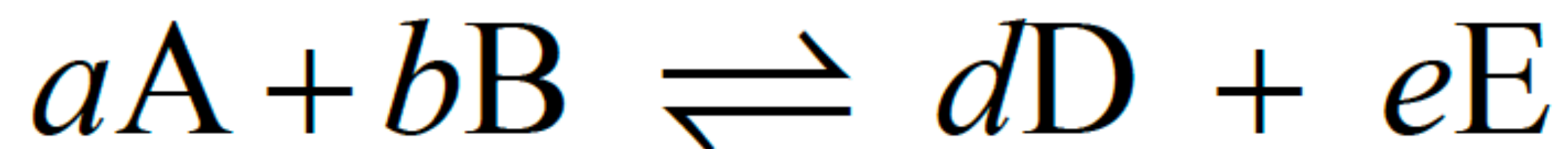
- K indicates how far a reaction will proceed towards the products at a given temperature.
- Small K means little to no reaction
- Large K means the reaction goes to or near completion
- Intermediate K means significant amounts of reactants and products are present at equilibrium.



The Reaction Quotient (Q)

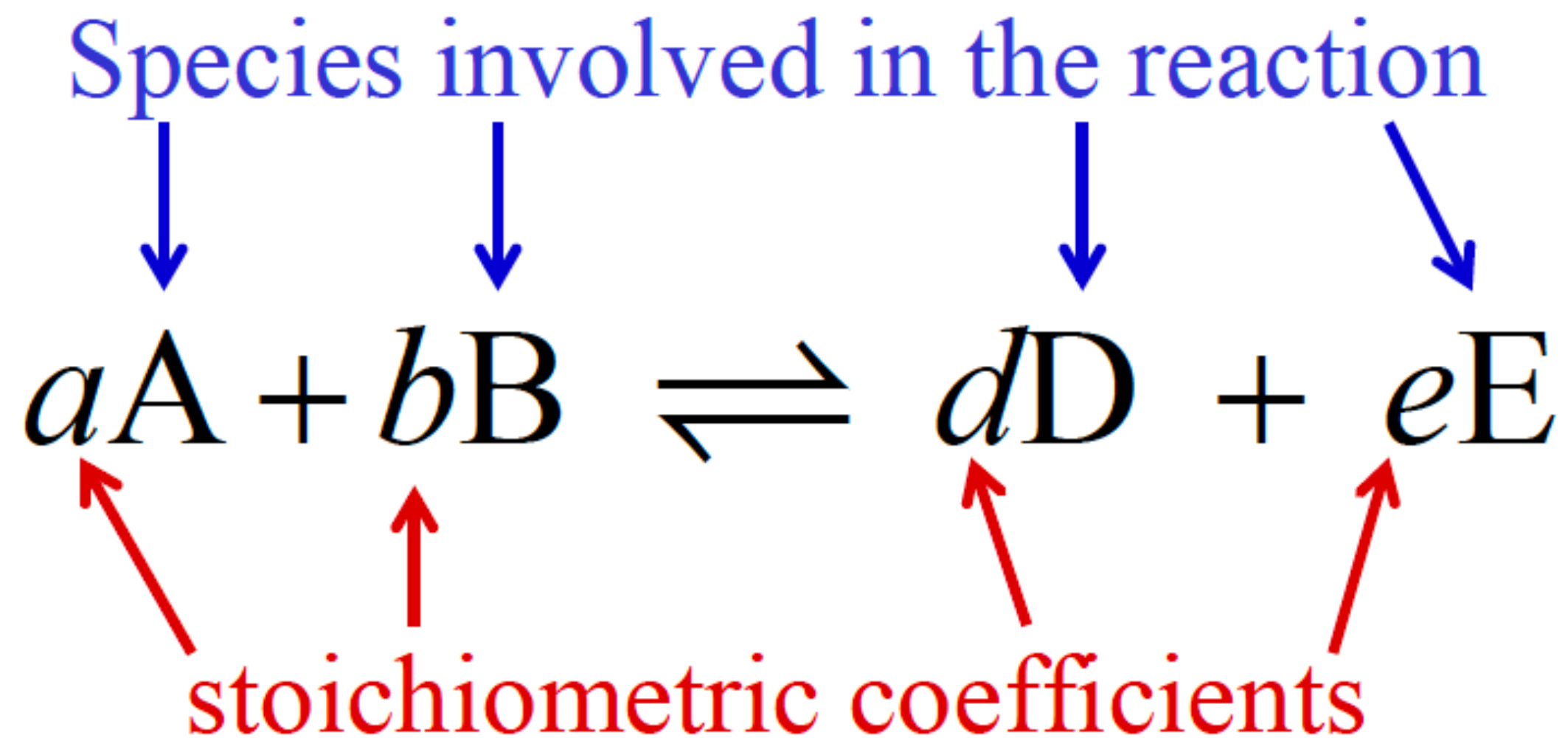
- The reaction quotient, Q_c , describes relative concentrations of products and reactants at any point in time.
- The expression for Q_c is the same as that for K_c .

- When the system is at equilibrium, $Q_c = K_c$
- When $Q_c < K_c$: The reaction will tend toward the products
- When $Q_c > K_c$: The reaction will tend toward the reactants



$$Q_c = \frac{[D]^d [E]^e}{[A]^a [B]^b}$$

For gases, K_p is often used



$$K_p = \frac{(P_D)^d (P_E)^e}{(P_A)^a (P_B)^b}$$

pressure constant

Partial Pressure measured in atm

For gases, K_p is often used

- The partial pressure of a gas in a system is the pressure exerted by that specific gas.
- The partial pressures of all the gases in a system sum up to the total pressure in that system.
- 1 mole of one type of gas will exert the same pressure as 1 mole of a different type of gas, under the same conditions of volume and temperature.
- 2 moles of a gas will exert twice as much pressure.

Example: Equilibrium Constant (K_p)

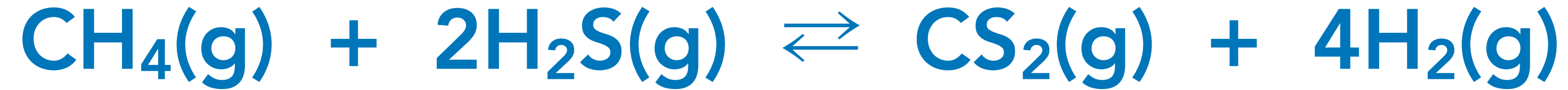
Write the equilibrium expression, K_p , for:



$$K_p = \frac{(P_{\text{NOCl}})^2}{(P_{\text{NO}_2})^2 (P_{\text{Cl}_2})}$$

You must use round brackets in the K_p expression.

Example: Equilibrium Constant (K_p)



- At 1000 K, the equilibrium partial pressures for the reaction above are $\text{CH}_4 = 0.20$ atm, $\text{H}_2\text{S} = 0.25$ atm, $\text{CS}_2 = 0.52$ atm and $\text{H}_2 = 0.10$ atm. What is K_p ?

Practice

For the reaction $\text{N}_2\text{O}_4(\text{g}) \rightleftharpoons 2\text{NO}_2(\text{g})$, $K_c = 0.21$ at 100°C . At a point during the reaction, $[\text{N}_2\text{O}_4] = 0.12 \text{ M}$ and $[\text{NO}_2] = 0.55 \text{ M}$. Is the reaction at equilibrium at that time? If not, in which direction is it proceeding?

Answer:

$$Q_c = [\text{NO}_2]^2/[\text{N}_2\text{O}_4] = (0.55)^2/(0.12) = 2.52$$

$2.52 \neq 0.21$ so it is not at equilibrium, and since $2.52 > 0.21$, the rxn must proceed to the LEFT, making more reactants to reach equilibrium.

7.4 Calculating the Equilibrium Constant

**7.5 Magnitude of the Equilibrium
Constant**

7.6 Properties of the Equilibrium Constant

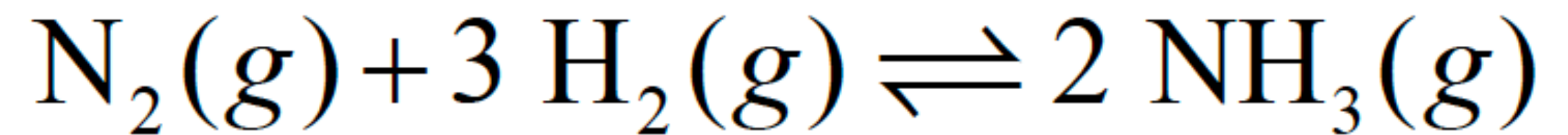
Example: Calculating K_c

A system establishes equilibrium at 500.0°C in accordance with the chemical equation below and the following concentrations were measured. Calculate the value of the equilibrium constant, K_c .

$$[\text{N}_2] = 1.50 \times 10^{-5} \text{ M}$$

$$[\text{H}_2] = 3.45 \times 10^{-1} \text{ M}$$

$$[\text{NH}_3] = 2.00 \times 10^{-4} \text{ M}$$



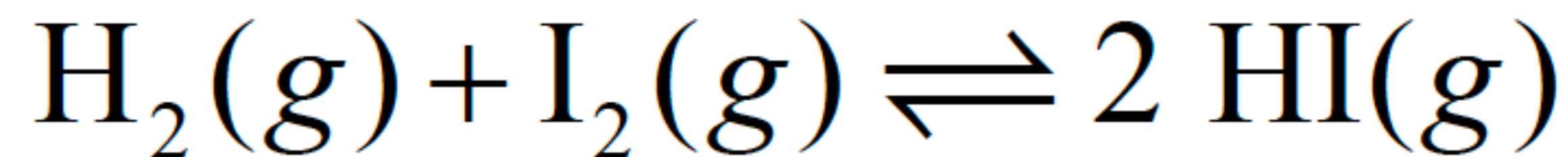
Example: Calculating K_p

A system establishes equilibrium at 485°C in accordance with the chemical equation below and the following partial pressures were measured. Calculate the value of the equilibrium constant, K_p .

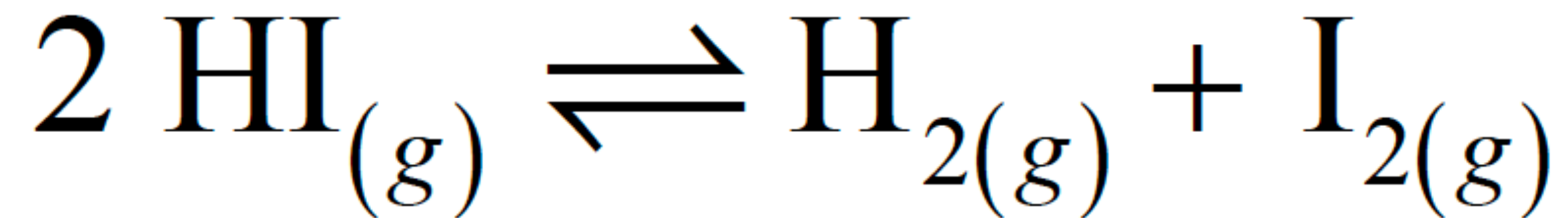
$$[\text{H}_2] = 0.035 \text{ atm}$$

$$[\text{I}_2] = 0.045 \text{ atm}$$

$$[\text{HI}] = 0.280 \text{ atm}$$



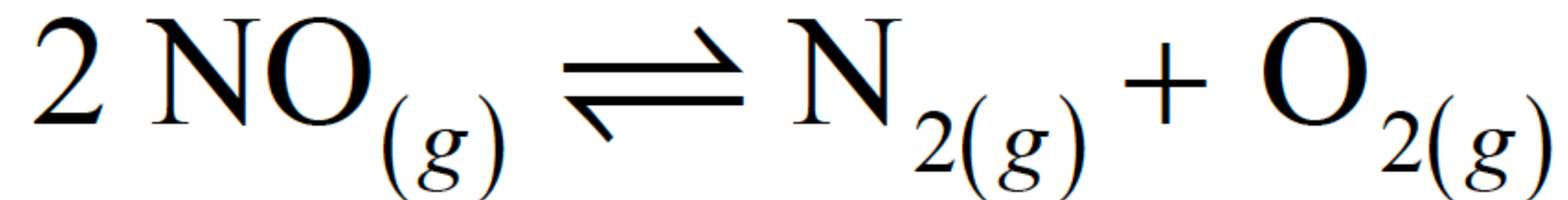
What K_{eq} Tells Us



$$K_P = \frac{(P_{\text{H}_2})(P_{\text{I}_2})}{(P_{\text{HI}})^2} = 0.0184 \text{ at } 698 \text{ K}$$

$(P_{\text{HI}})^2 > (P_{\text{H}_2})(P_{\text{I}_2})$
Mostly Reactants

What K_{eq} Tells Us



$$K_c = \frac{[\text{N}_2][\text{O}_2]}{[\text{NO}]^2} = 2.4 \times 10^3 \quad \text{at } 2273 \text{ K}$$

$$[\text{NO}]^2 \ll [\text{N}_2][\text{O}_2]$$

Mostly Products

What K_{eq} Tells Us

$K_{eq} \gg 1$ (mostly products)
(equilibrium lies far to the right)

$K_{eq} \ll 1$ (mostly reactants)
(equilibrium lies far to the left)

$K_{eq} \approx 1$ (\sim equal amounts of each)
(equilibrium lies in the middle)

Manipulating K & Q

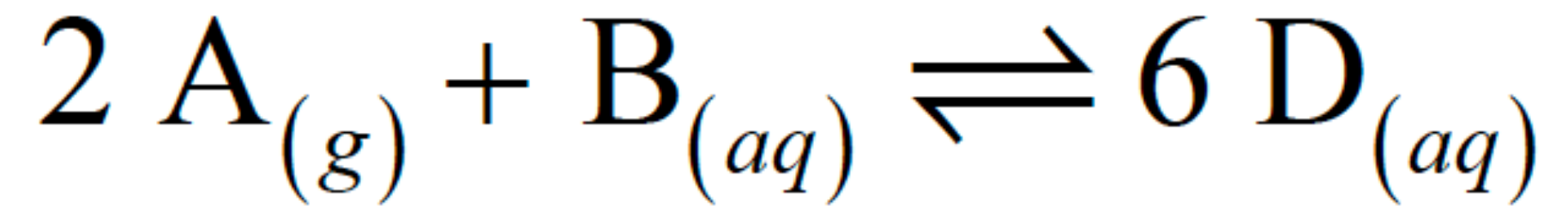
There are three ways in which K and Q can be manipulated.

1. Coefficient Rule
2. Reciprocal Rule
3. Multiple Equilibria Rule

Coefficient Rule

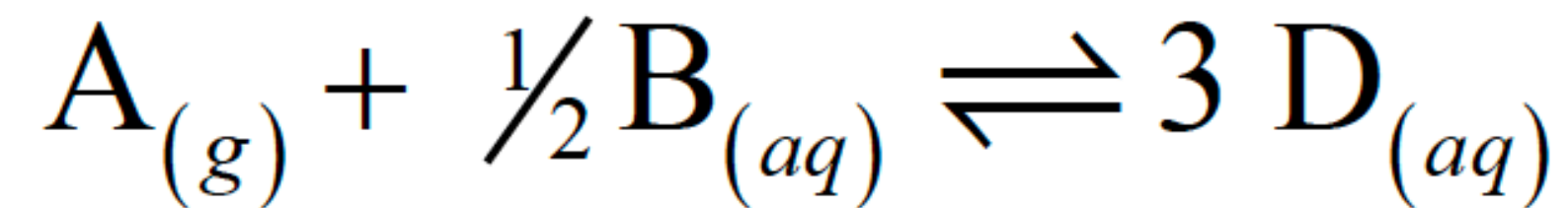
When coefficients are changed by a factor of n , K_{eq} is raised to the power of n .

(i)



$$K_c^i = \frac{[D]^6}{[A]^2[B]}$$

$\frac{1}{2}$ (i) = (ii)



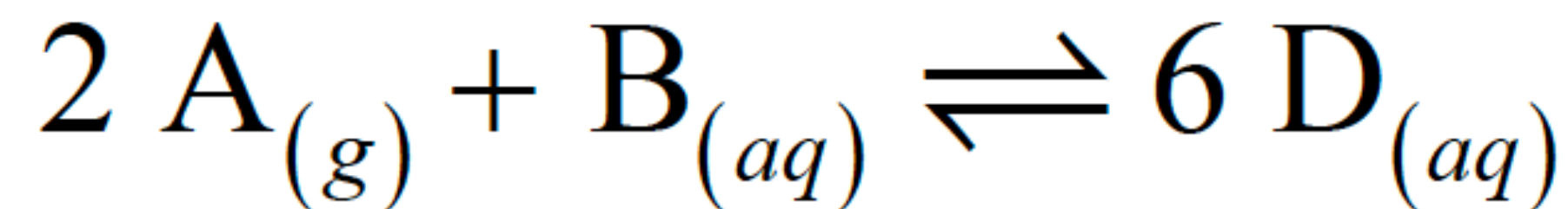
$$K_c^{ii} = \frac{[D]^3}{[A][B]^{\frac{1}{2}}} = \left[\frac{[D]^6}{[A]^2[B]} \right]^{\frac{1}{2}}$$

$$K_c^{ii} = (K_c^i)^{\frac{1}{2}}$$

Reciprocal Rule

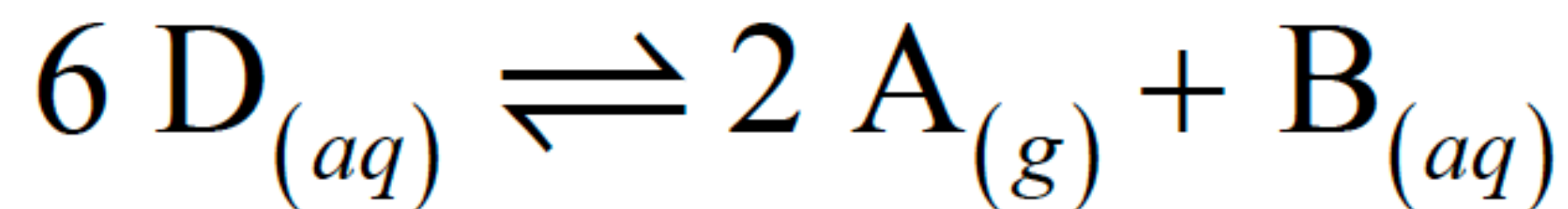
When a reaction is reversed, the new K_{eq} value is the inverse of the old K_{eq} value.

(i)



$$K_c^i = \frac{[D]^6}{[A]^2[B]}$$

(i)⁻¹ = (iii)

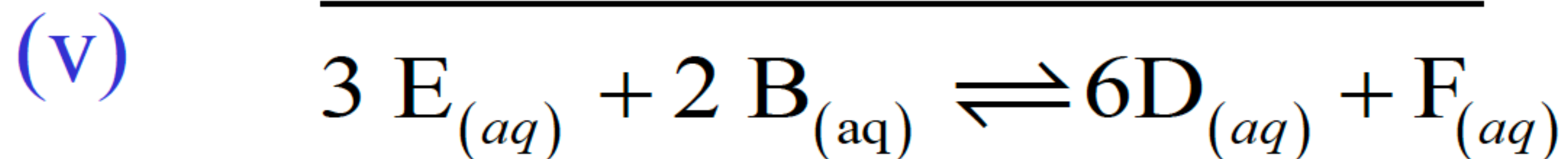
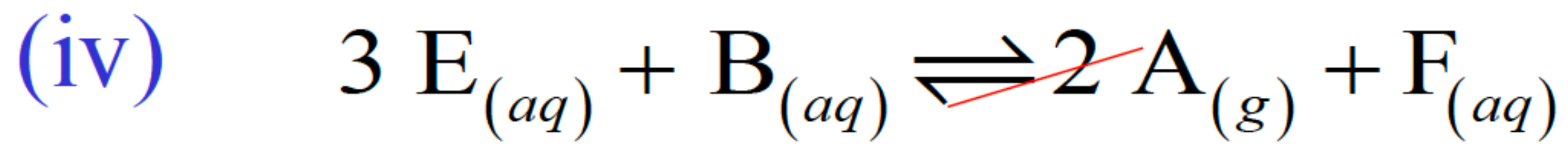
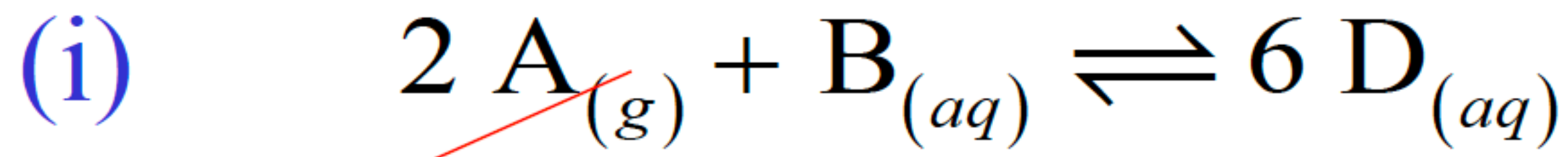


$$K_c^{iii} = \frac{[A]^2[B]}{[D]^6}$$

$$K_c^{iii} = 1 / K_c^i$$

Multiple Equilibria Rule

When two or more reactions are combined, the new K_{eq} is the product of the K_{eq} values from the individual reactions.



$$\frac{[D]^6}{[A]^2 [B]} \times \frac{[A]^2 [F]}{[E]^3 [B]} = \frac{[D]^6 [F]}{[E]^3 [B]^2}$$

$$K_c^i \times K_c^{iv} = K_c^v$$

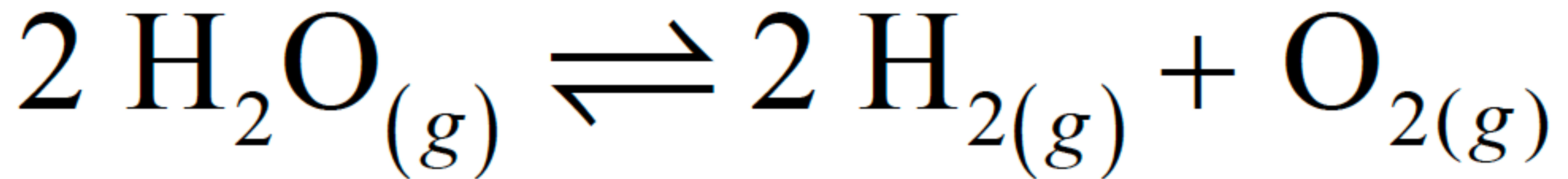
7.7 Calculating Equilibrium Concentrations

- Calculating Equilibrium Partial Pressures & Concentration
- ICE Charts

Warm-up: Calculating Equilibrium Partial Pressures

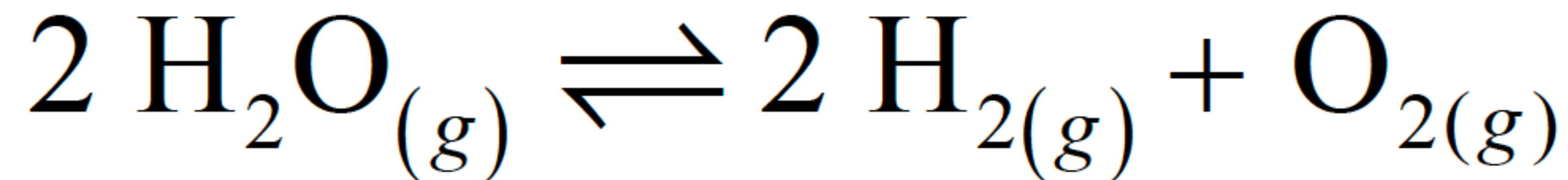
Suppose you start out with only $\text{H}_2\text{O}(g)$ in a rigid container at 25°C , and its initial partial pressure is recorded to be 0.784 atm . What are the partial pressures of each species when the system reaches equilibrium?

$$(K_p = 2.0 \times 10^{-42})$$



Warm-up: Calculating Equilibrium Partial Pressures

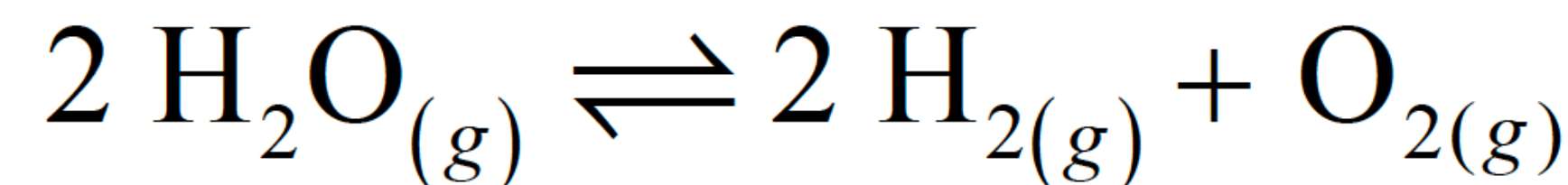
($K_p = 2.0 \times 10^{-42}$)



Initial	0.784	0	0
Change	-2x	+2x	+x
Equilibrium	0.784 - 2x	2x	x

Warm-up: Calculating Equilibrium Partial Pressures

$$(K_p = 2.0 \times 10^{-42})$$



Initial	0.784	0	0
Change	-2x	+2x	+x
Equilibrium	0.784 - 2x	2x	x

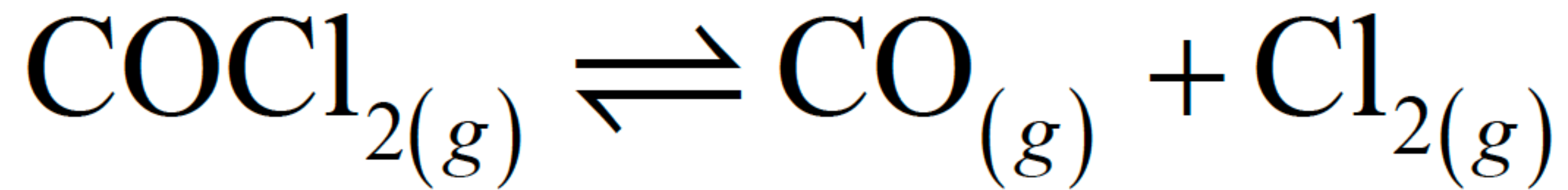
$$K_p = \frac{(P_{\text{H}_2})^2 (P_{\text{O}_2})}{(P_{\text{H}_2\text{O}})^2} = \frac{(2x)^2 (x)}{(0.784 - 2x)^2}$$

$$2.0 \times 10^{-42} = \frac{4x^3}{(0.784)^2} \quad \text{○}$$

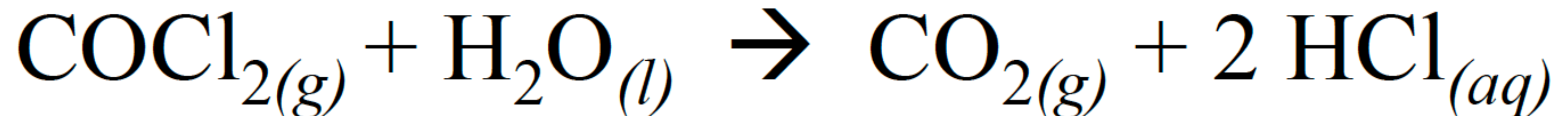
When $K_{\text{eq}} < 1 \times 10^{-4}$
you can usually ignore
this (x) to avoid the
difficult math.

Example: Calculating Equilibrium Concentrations

Find the equilibrium concentrations of all species if 0.194 mol of COCl_2 is allowed to come to equilibrium in a 5.8 L container at 25°C . ($K_c = 7.28 \times 10^{-38}$)



Initial	3.3×10^{-2}	0	0
Change	-x	+x	+x
Equilibrium	$3.3 \times 10^{-2} - x$	x	x



7.8 Representations of Equilibrium

7.9 Introduction to Le Chatelier's Principle

**7.10 Reaction Quotient & Le Chatelier's
Principle**

Le Chatelier's Principle

When a system at equilibrium is subjected to a stress, the equilibrium will shift in order to reduce that stress.

The only three stresses are changes in:

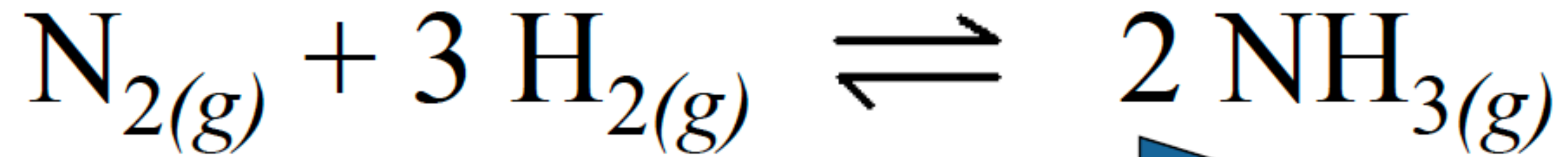
1. Pressure
2. Concentration
3. Temperature

Stress from Increasing Pressure

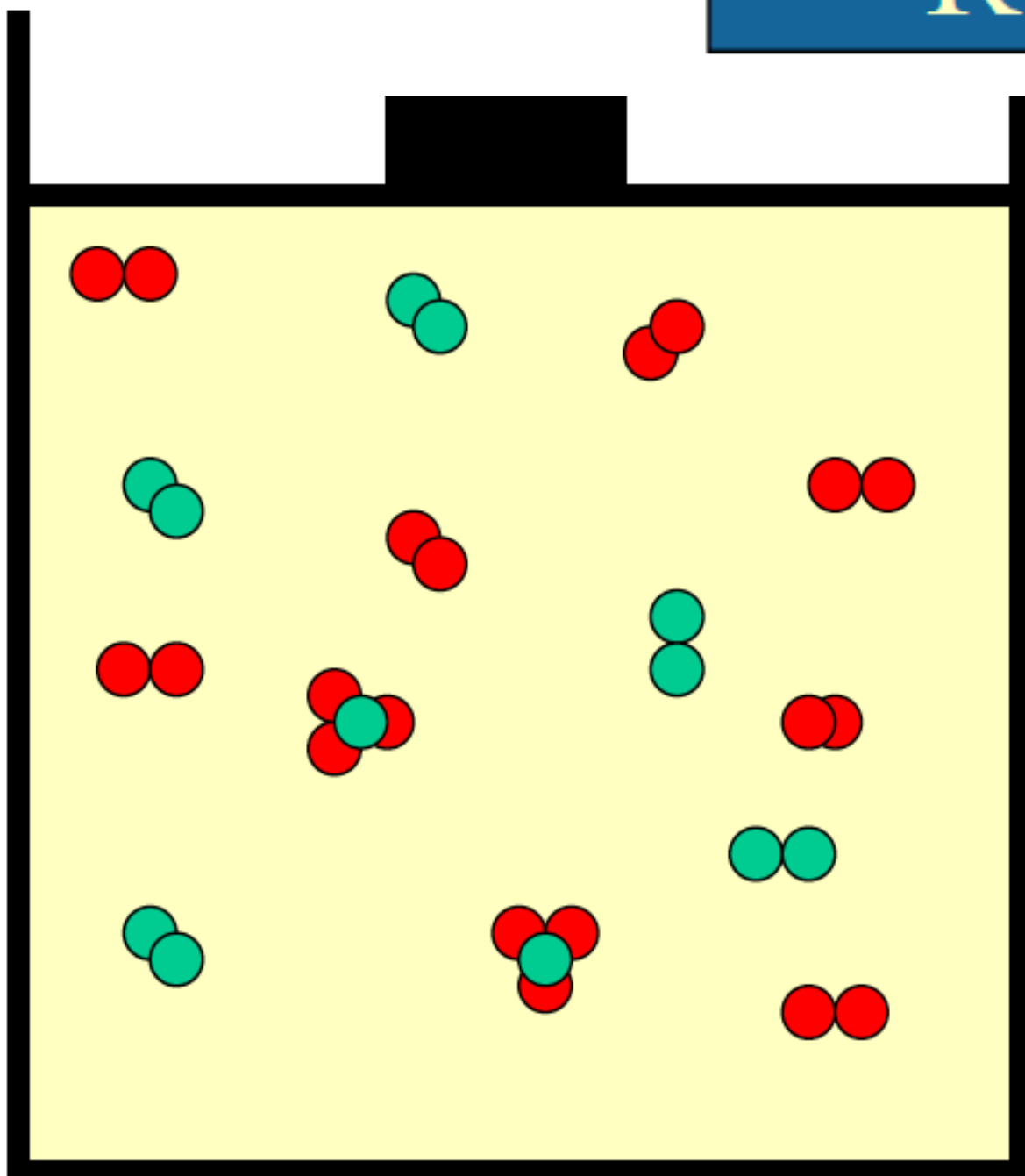
If the **pressure** on a system at equilibrium is **increased**, Q changes and the reaction will proceed toward the side with **fewer moles of gas** to reduce the stress.

This changes the equilibrium concentrations, but it **does not** change the Equilibrium Constant (K_{eq}).

Stress from Increasing Pressure

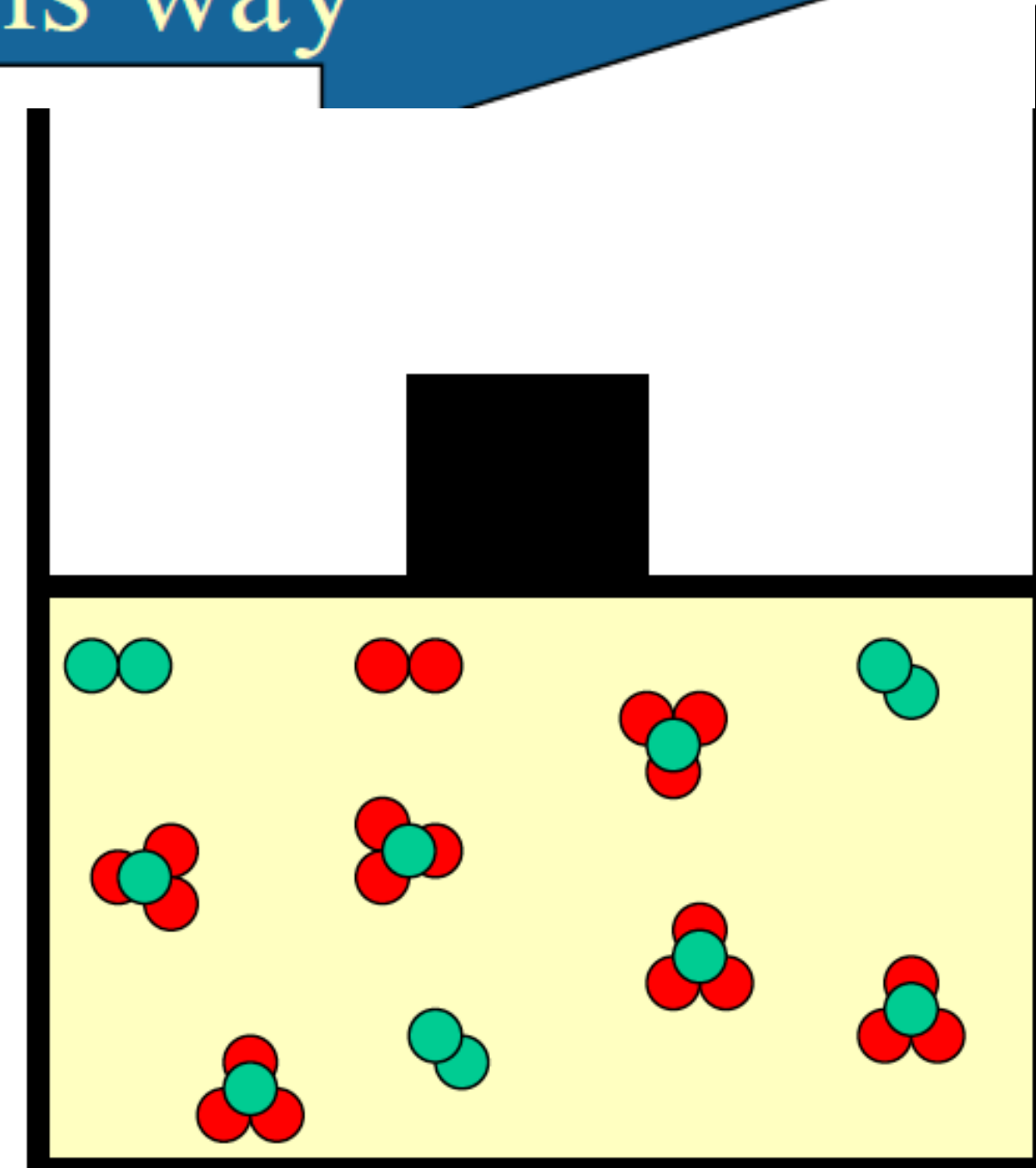


Reaction proceeds this way



14 gaseous molecules

2 NH_3 , 5 N_2 , 7 H_2



10 gaseous molecules

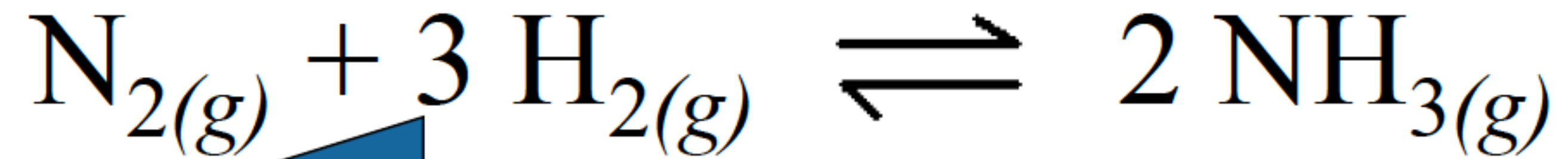
6 NH_3 , 3 N_2 , 1 H_2

Stress from Decreasing Pressure

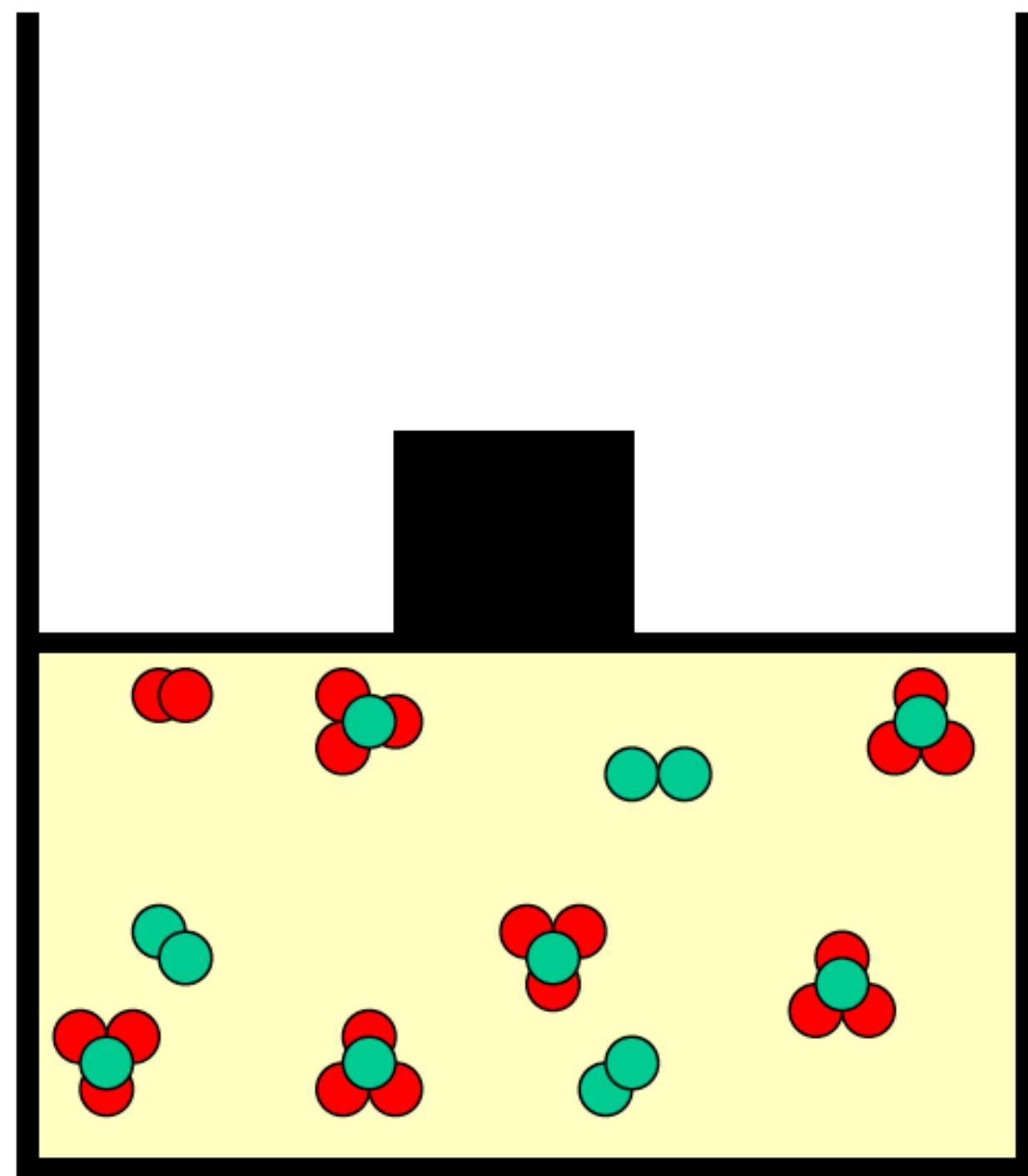
If the **pressure** on a system at equilibrium is **decreased**, Q changes and the reaction will proceed toward the side with **more moles of gas** to reduce the stress.

This changes the equilibrium concentrations, but it **does not** change the Equilibrium Constant (K_{eq}).

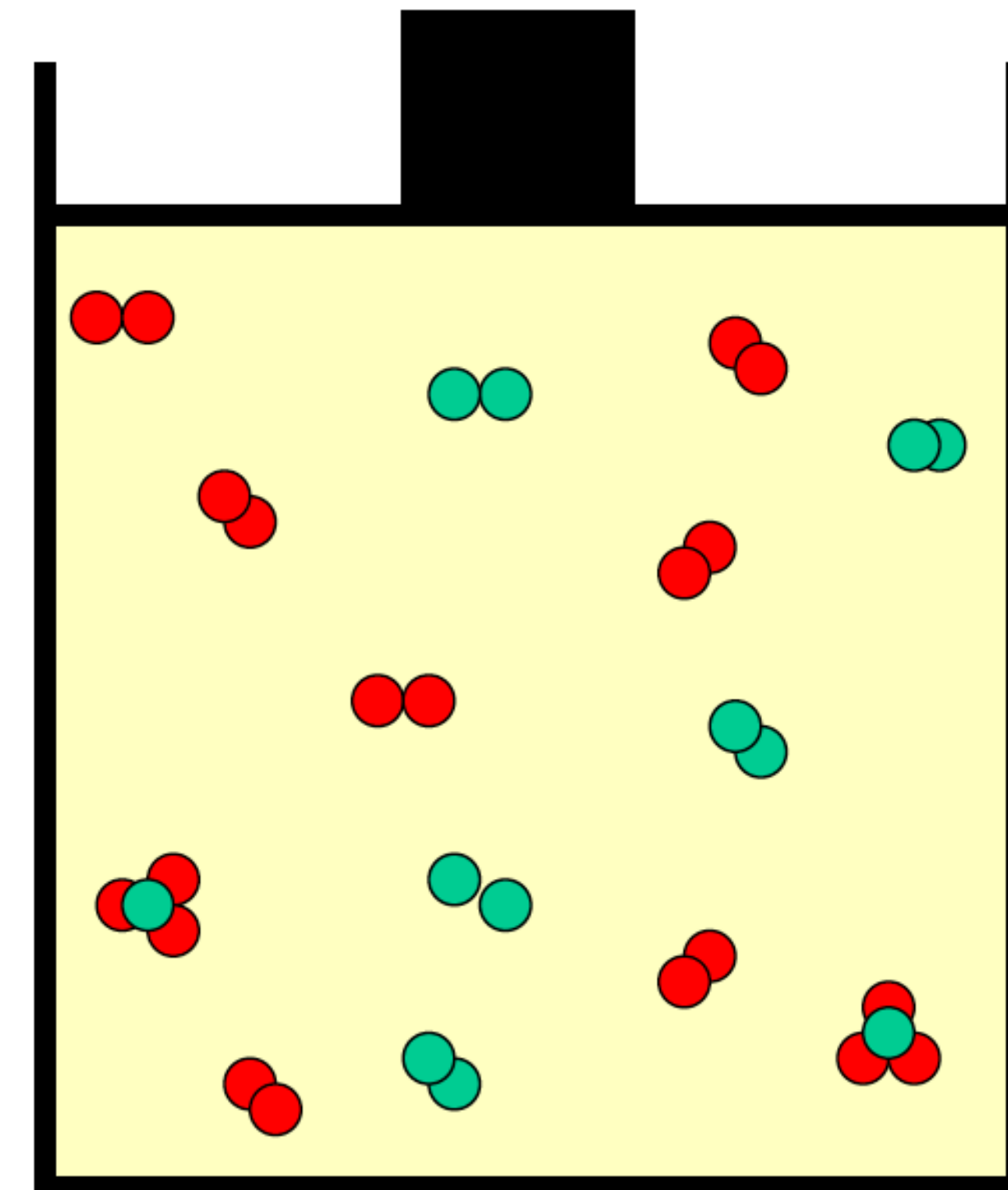
Stress from Decreasing Pressure



Reaction proceeds this way



10 gaseous molecules



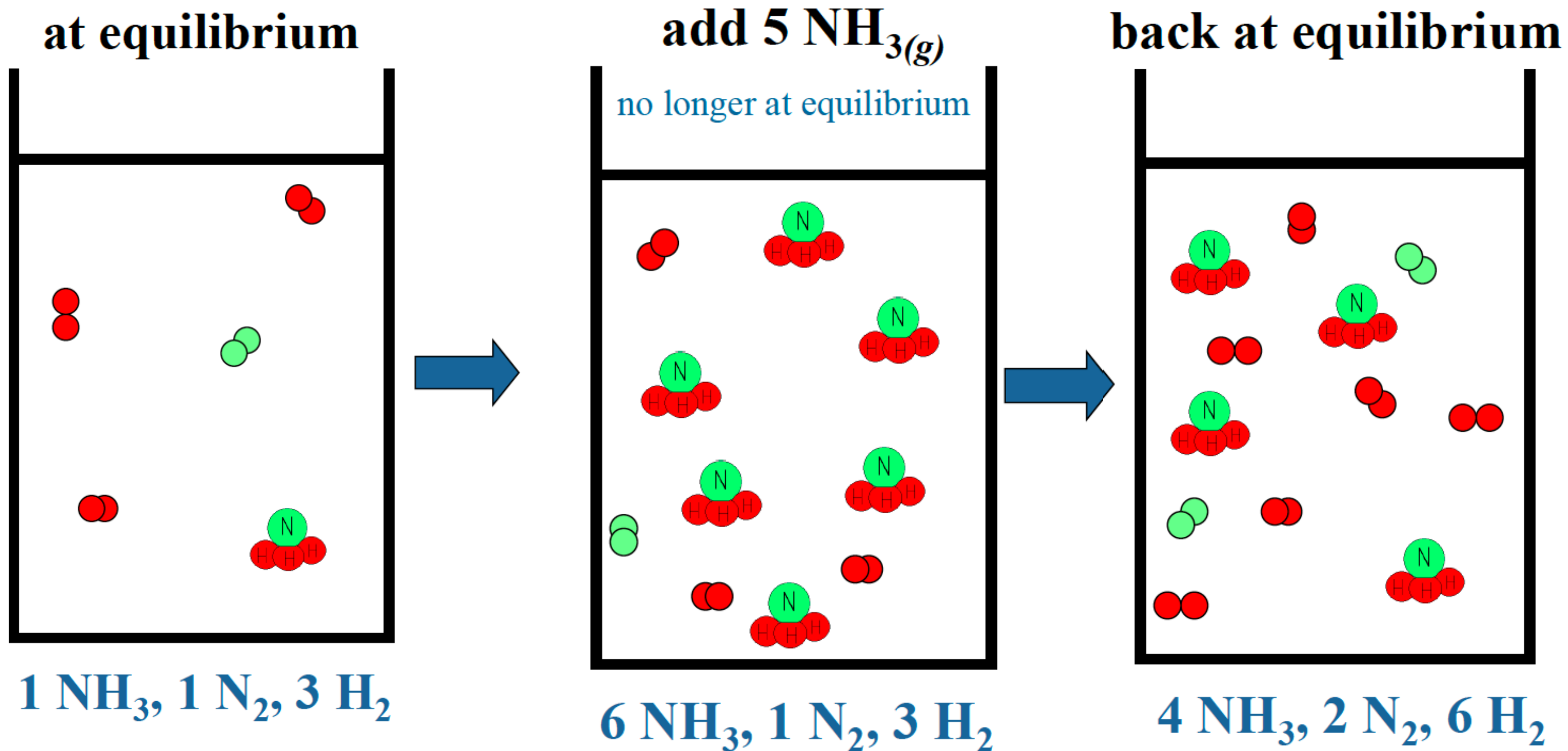
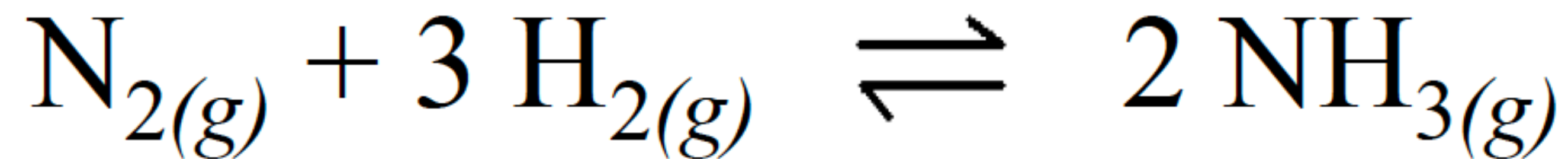
14 gaseous molecules

Stress from Increasing Concentration

If the **concentration** on a system at equilibrium is **increased**, Q changes and the reaction will proceed in the direction that will **reduce the concentration** of that species.

This increases the equilibrium concentrations, but it does not change the Equilibrium Constant (K_{eq}).

Adding more NH₃ to the system



Stress from Decreasing Concentration

If the **concentration** on a system at equilibrium is **decreased**, Q changes and the reaction will proceed in the direction that will **increase the concentration** of that species.

This increases the equilibrium concentrations, but it does not change the Equilibrium Constant (K_{eq}).

Stress from Dilution

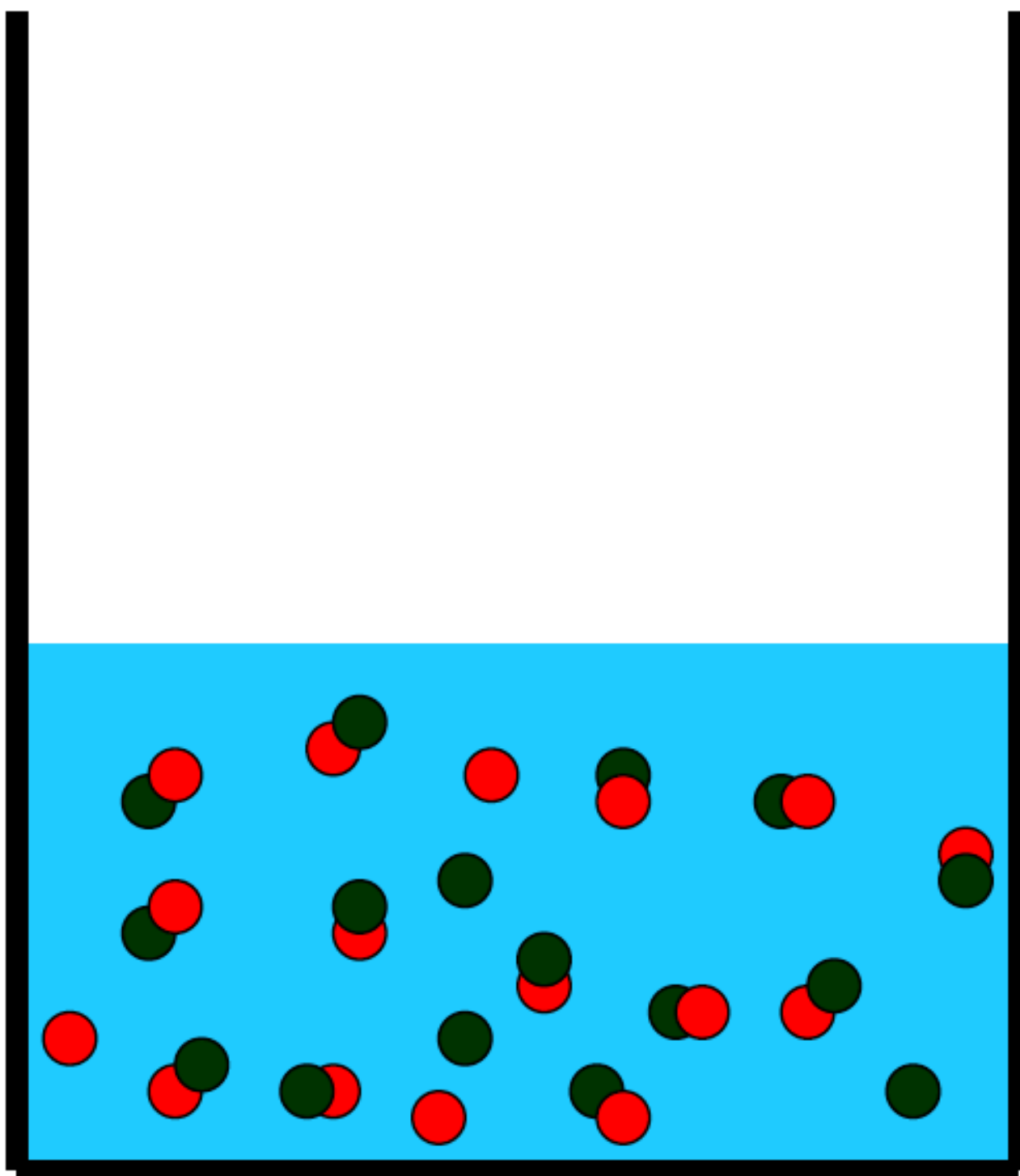
If **solvent is added** to a system at equilibrium, Q changes and the reaction will proceed toward the side with **more particles** to reduce that stress.

This increases the equilibrium concentrations, but it **does not** change the Equilibrium Constant (K_{eq}).

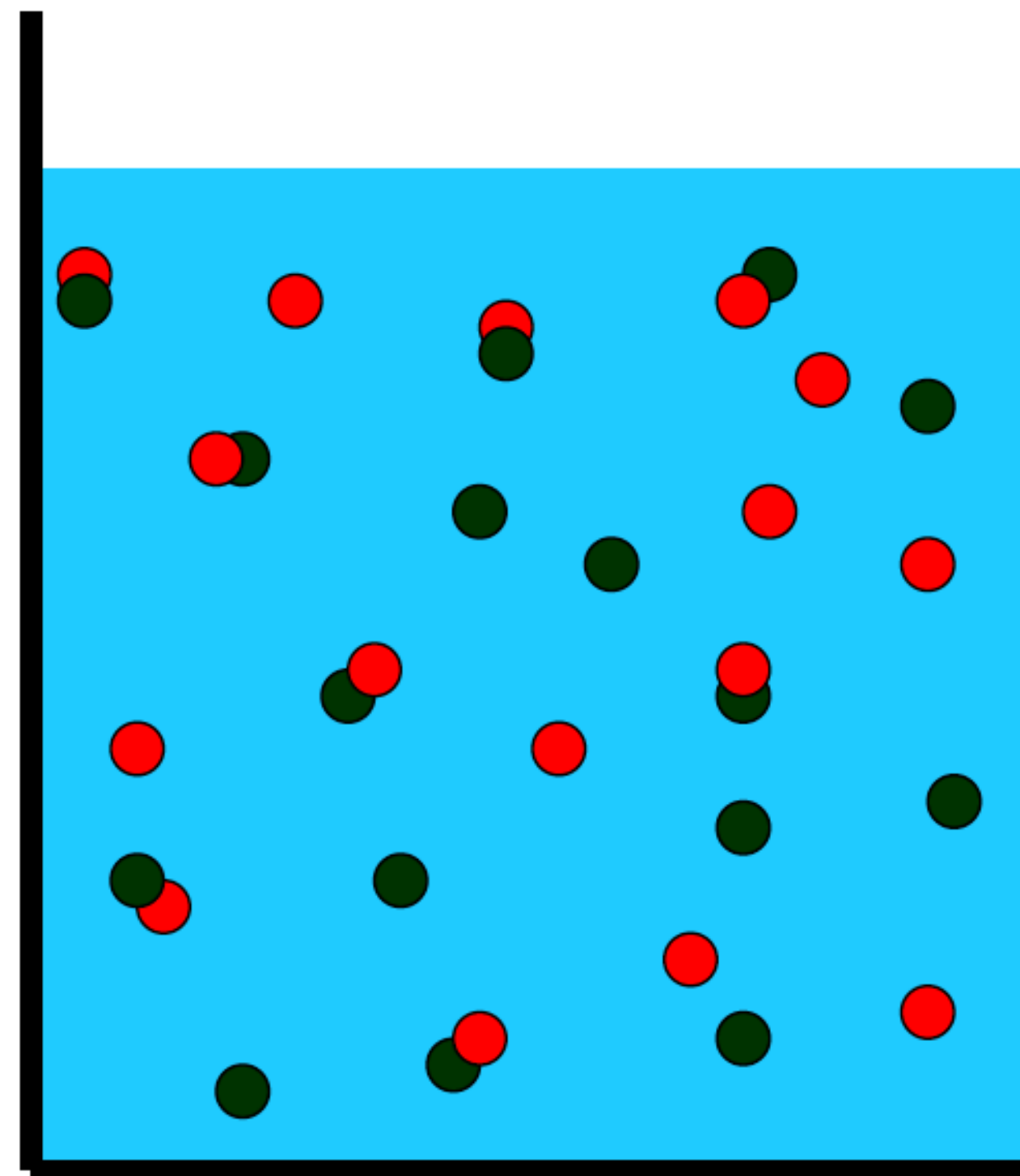
Stress from Dilution



Reaction will proceed this way



13 aqueous HF



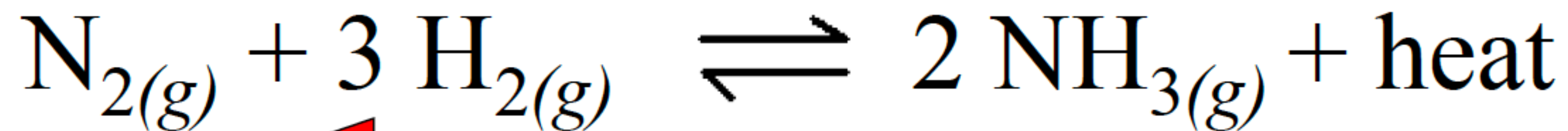
8 aqueous HF

Stress from Changing Temperature

This is the only stress that changes the equilibrium constant (K_{eq})



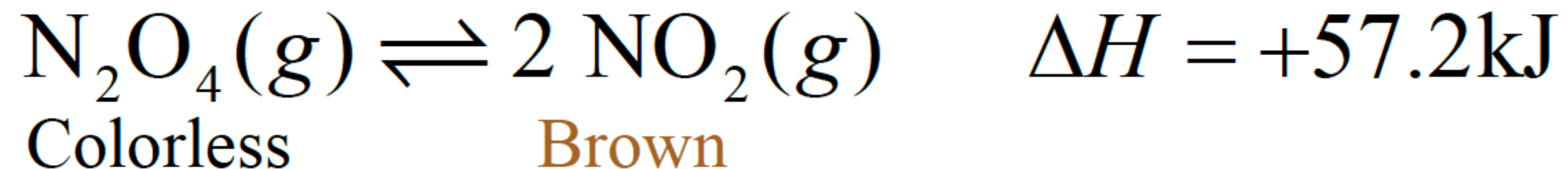
Cooling (taking heat away) shifts the equilibrium in the direction that produces heat.



Adding heat (increasing the temperature) shifts the equilibrium in the direction that absorbs heat.

Example: Stress from Temperature Changes

A system represented by the chemical equation below is in a state of equilibrium at 25°C. Describe the color change that would occur if the temperature of the system increases to 75°C.



- When heat is added, the reaction will proceed to the right.
- The system would become a darker shade of brown, because $[\text{NO}_2]$ would increase.

Example: Stress from Temperature Changes

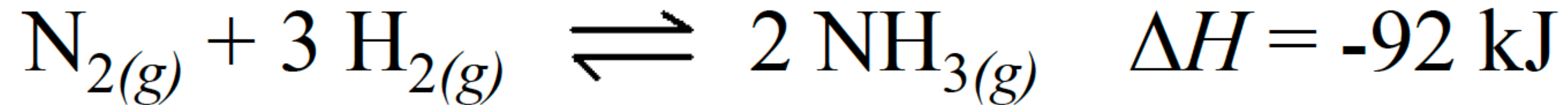
A system represented by the chemical equation below is in a state of equilibrium at 5°C. If the temperature of the system increases to 99.0°C, will the pH increase, decrease or remain the same?



- When heat is added, the reaction will proceed to the right.
- The pH would decrease, because $[\text{H}_3\text{O}^+]$ would increase.

Example: Stress from Temperature Changes

A system represented by the chemical equation below is in a state of equilibrium in a cylinder at 25.00°C. If the volume of the cylinder was increased, would the temperature increase, decrease or remain the same while the system attempts to re-establish equilibrium? Justify your answer.



- The temperature will decrease.
- The rate of the reverse reaction would be greater than the rate of the forward reaction.
- The reverse reaction is endothermic.

7.11 Introduction to Solubility Equilibria

7.12 Common-Ion Effect

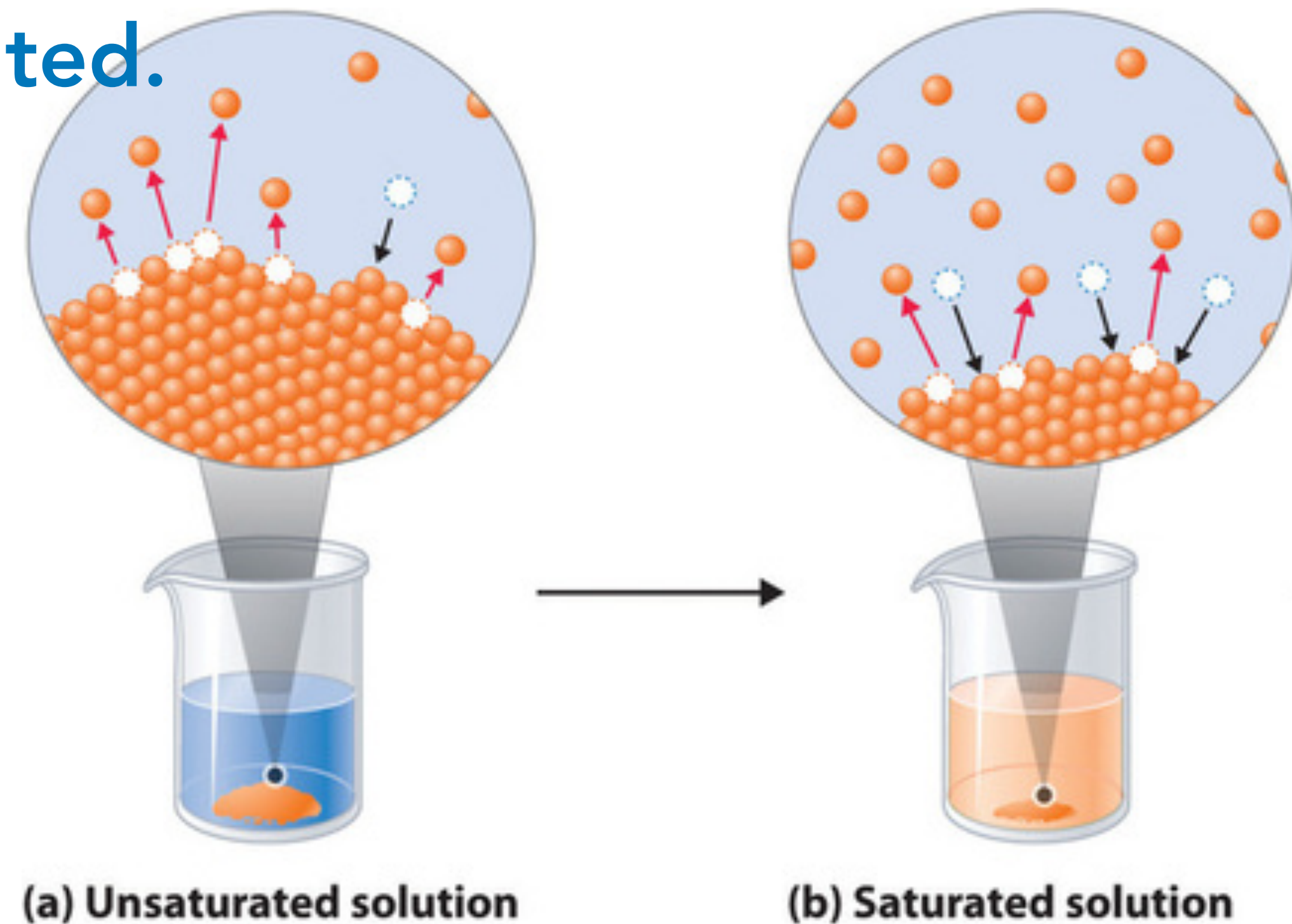
- The Solubility Product Constant (K_{sp})
- Predicting Precipitates

Saturation & Equilibrium

- **Saturated Solution**

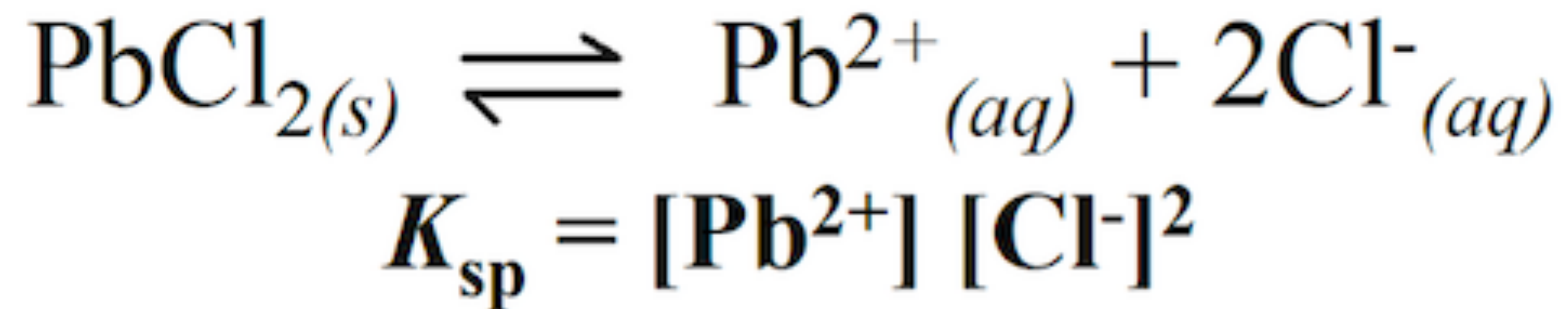
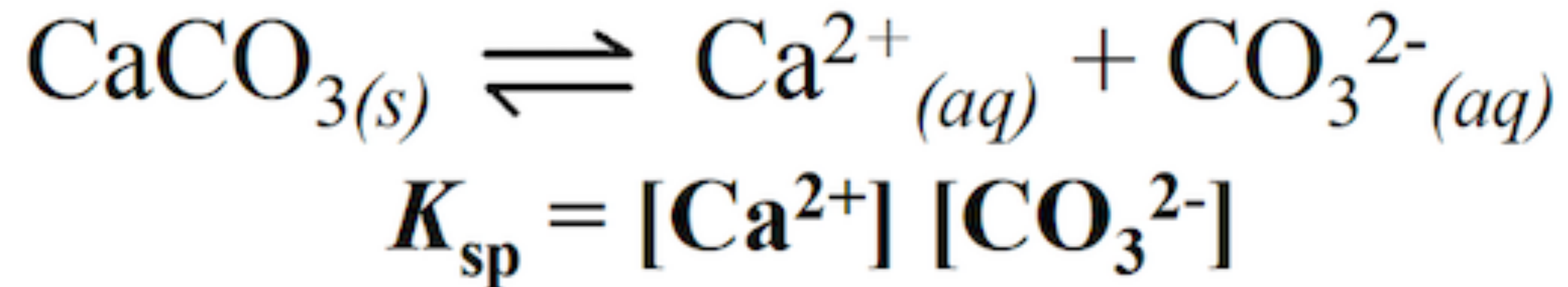
- The solvent has dissolved the maximum amount of solute that can at a certain temperature, and some solid solute remains on the bottom.

- A solution is at equilibrium when it is saturated.



The Solubility Product Constant (K_{sp})

- This is K_{sp} for ionic compounds in water.

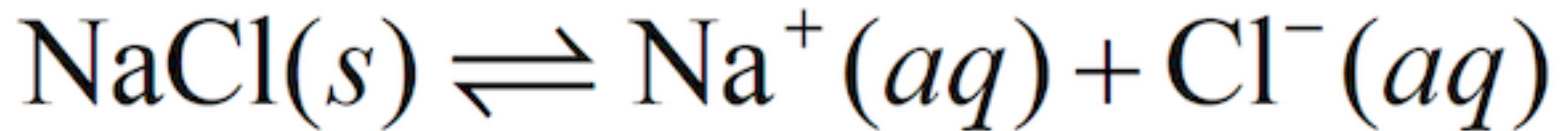


K_{sp} values generally range from about 1×10^{-3} to 1×10^{-54} or compounds that are considered to be insoluble. ONLY DEPENDENT ON TEMPERATURE

Solubility Rules

All salts containing **Na⁺, K⁺, NH₄⁺ or NO₃⁻** are soluble in water.

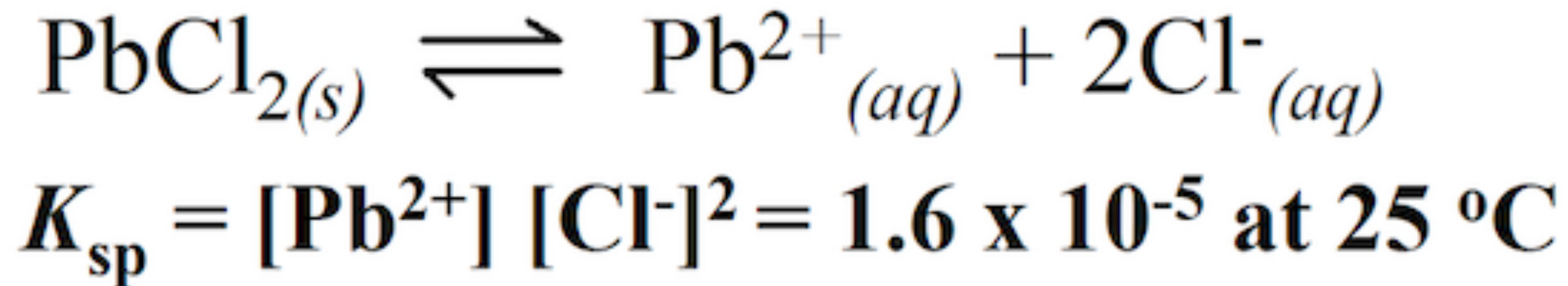
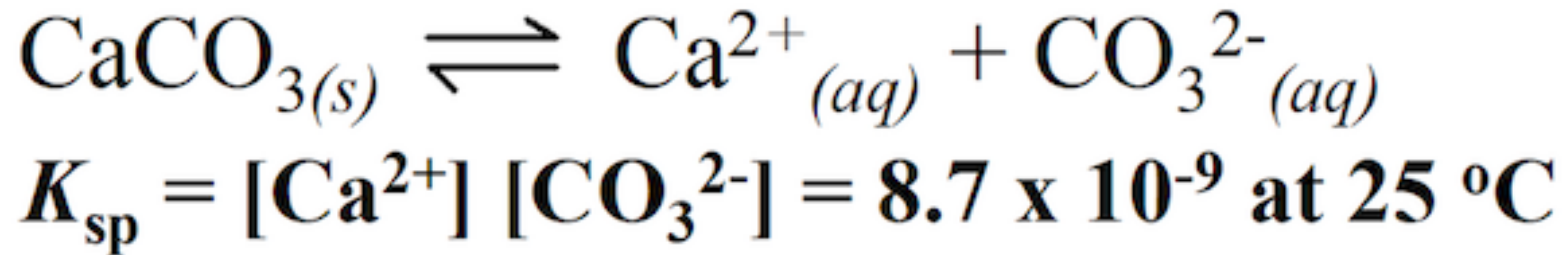
$K_{sp} > 1$ for all salts containing these ions, which is why they are considered soluble. The equilibrium lies to the right.



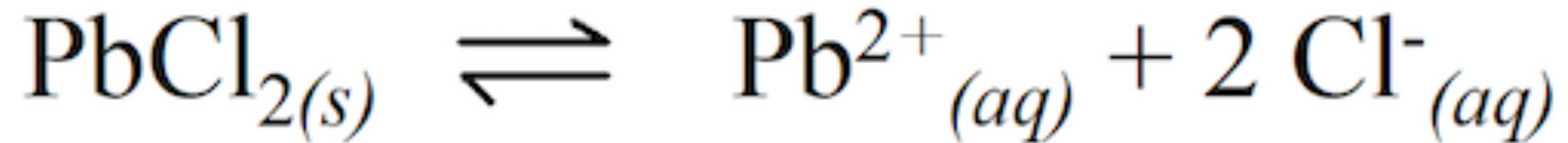
K_{sp} determines the amount of dissociation that occurs as a reaction proceeds at equilibrium.

Example #1

Which compound is the least soluble in water at 298K?



Solubility

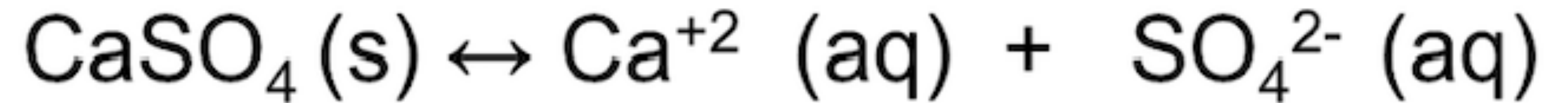


- The solubility is the maximum molar concentration of formula units that will dissolve at a given temperature.
- For every 1 mole of $\text{PbCl}_2(s)$ that dissolves, 1 mole of Pb^{2+} ions and 2 moles of Cl^{-} ions enter the solution.
- Solubility of $\text{PbCl}_2 = [\text{Pb}^{2+}] = 1/2[\text{Cl}^{-}]$
 - When the **solution is saturated**.

Example: K_{sp} Calculation

- The solubility product constant for lead (II) fluoride is 3.6×10^{-8} at 25°C .
 - (a) Write the balanced chemical equation.
 - (b) Write the equilibrium expression
 - (c) Find the maximum molar concentration of the ions in solution and the molar solubility (s) of the solution.

Practice: The solubility of CaSO_4 is found to be 0.67 g/L. Calculate the value of K_{sp} for calcium sulfate.



Initial		0	0
Change	-s	+s	+s
Equilibrium		s	s

Step 1: Calculate the number of moles of CaSO_4 dissolved in 1 L of solution.

Step 2: Substitute into the K_{sp} expression.

K_{sp} & Q_{sp}

If $Q_{sp} = K_{sp}$

- The system is at equilibrium
- It is a saturated solution with solid and aqueous species.

If $Q_{sp} > K_{sp}$, a precipitate will form

- The reaction will proceed to the left until the system reaches equilibrium

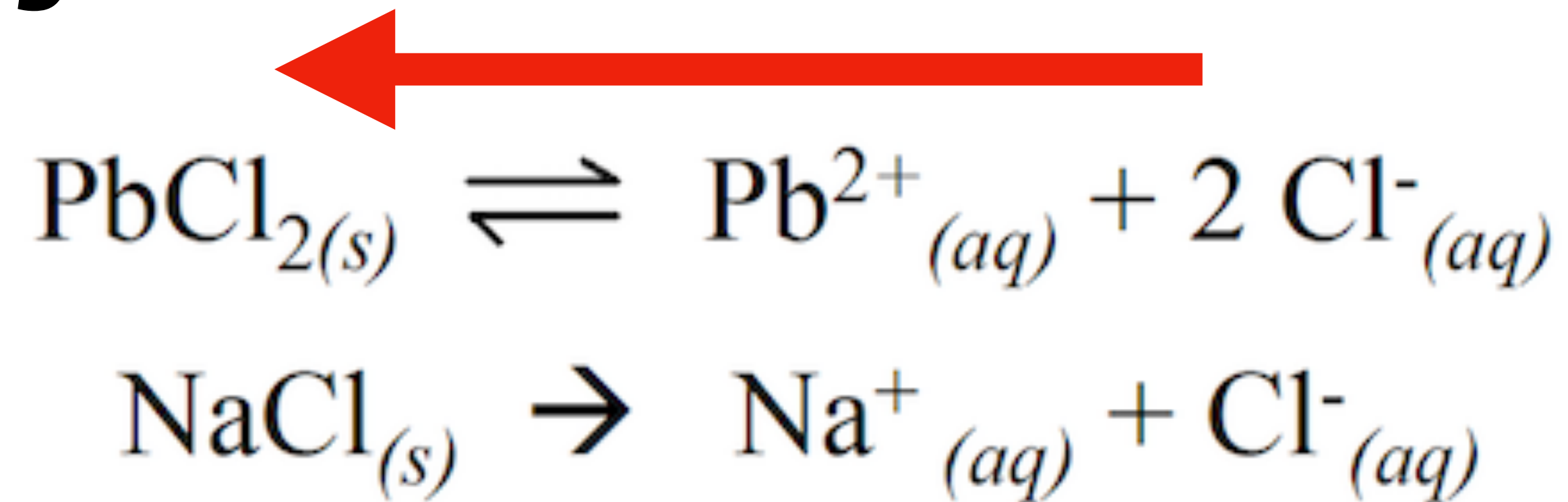
If $Q_{sp} < K_{sp}$, no precipitate forms.

- The solution is unsaturated.
- All of the ions will remain in solution.

Example: Predicting Possible Precipitates

- (a) Find K_{sp} for a saturated solution of $PbCl_2$ if the concentration of Cl^- is found to be 0.0325 M.
- (b) Will a precipitate of $PbCl_2$ form when 200.0 mL of $3.78 \times 10^{-2} M$ NaCl is mixed with 100.0 mL of $2.45 \times 10^{-2} M$ $Pb(NO_3)_2$. Assume that the temperature of the resulting solution is the same as that from part a.

Solubility & the Common Ion Effect



- Cl^{-} is the common ion that causes the equilibrium in the first reaction to shift
- The presence of a common ion **decreases** the solubility of the salt.
- At a given temperature, K_{sp} depends on the product of the ion concentration. If the concentration of either ion goes up, the other will go down to maintain K_{sp} .

Example: Common Ion Effect

- (a) Find $[\text{Ba}^{2+}]$ and $[\text{SO}_4^{2-}]$ after 0.0200 g of $\text{Ba}(\text{NO}_3)_2$ is added to a 400.0 mL saturated solution of BaSO_4 and equilibrium is established. Assume that the volume remains the same and the final temperature is 25°C . ($K_{\text{sp}} = 1.1 \times 10^{-10}$ for BaSO_4 at 25°C)

Example: Predicting Precipitates & the Common Ion Effect

If 0.15 M NaOH is slowly poured into a beaker containing 0.14 M $\text{Ca}(\text{NO}_3)_2$ and 0.25 M $\text{Fe}(\text{NO}_3)_2$, which precipitate will form first?

$$K_{\text{sp}} \text{ for } \text{Ca}(\text{OH})_2 = 8.0 \times 10^{-6}$$

$$K_{\text{sp}} \text{ for } \text{Fe}(\text{OH})_2 = 1.6 \times 10^{-14}$$

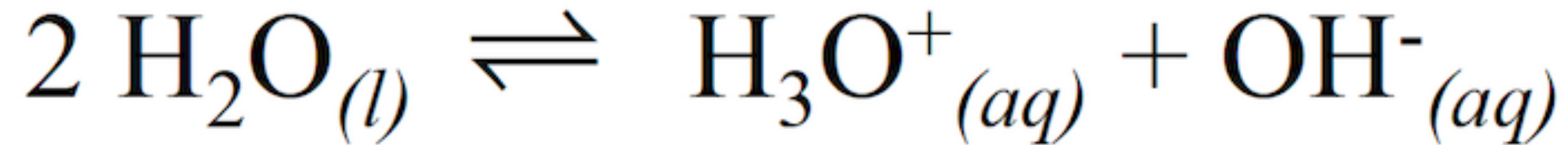
Step 1: Find $[\text{OH}^-]_{\text{max}}$ for $\text{Ca}(\text{OH})_2$

Step 2: Find $[\text{OH}^-]_{\text{max}}$ for $\text{Fe}(\text{OH})_2$

7.13 pH & Solubility

- pH & Soluble Salts
- Solubility in Weak & Strong Acid Solutions

Autoionization of Water



In pure water at 25°C,

$[\text{H}_3\text{O}^+] = 1.0 \times 10^{-7}$ and $[\text{OH}^-] = 1.0 \times 10^{-7}$.

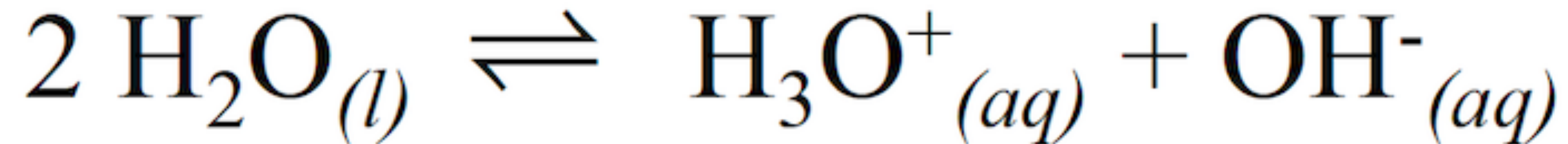
As $[\text{H}_3\text{O}^+] = [\text{OH}^-]$ the solution is neutral.

$$K_w = [\text{H}_3\text{O}^+] [\text{OH}^-]$$

$$K_w = (1.0 \times 10^{-7}) (1.0 \times 10^{-7})$$

$$K_w = 1.0 \times 10^{-14} \quad (\text{at } 25 \text{ }^\circ\text{C})$$

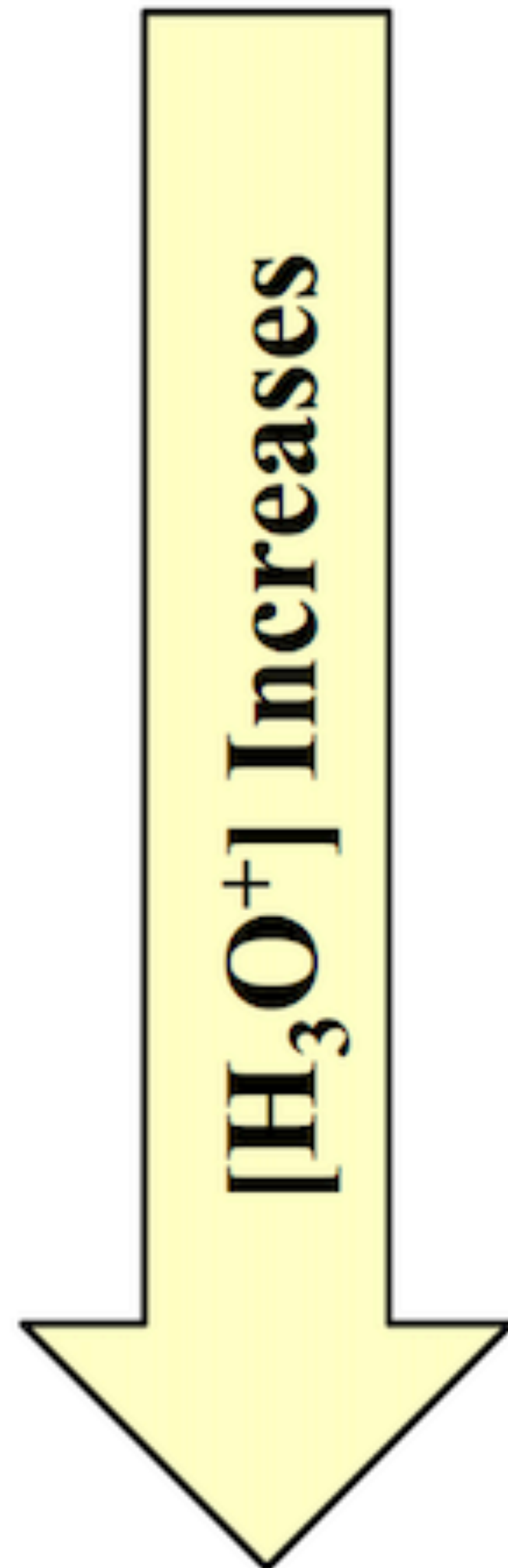
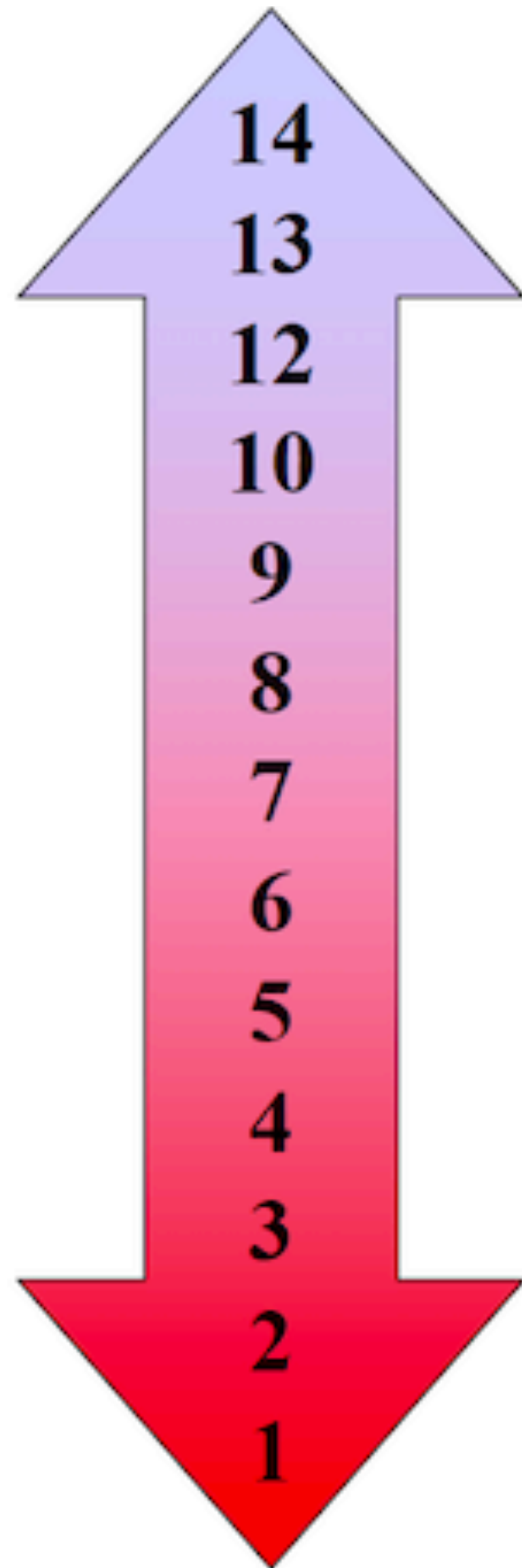
Autoionization of Water



$$K_w = [\text{H}_3\text{O}^+] [\text{OH}^-] = 1.0 \times 10^{-14} \quad (\text{at } 25 \text{ }^\circ\text{C})$$

- This is a constant.
- If you know the concentration of $[\text{H}_3\text{O}^+]$ you can calculate the concentration of $[\text{OH}^-]$ or vice versa.
- Memorize this constant! It's very useful.

The pH Scale

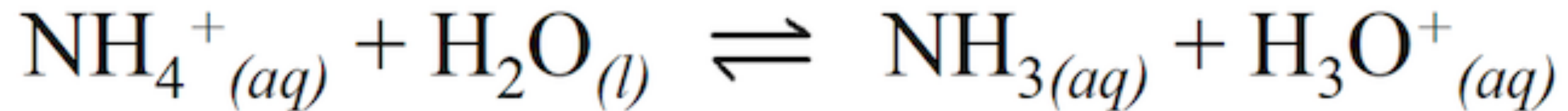


The pH of a solution increases as $[\text{H}_3\text{O}^+]$ decreases and $[\text{OH}^-]$ increases.

The pH of a solution decreases as $[\text{H}_3\text{O}^+]$ increases and $[\text{OH}^-]$ decreases.

Some Cations Acidify Solutions

- Ionic compounds containing NH_4^+ can acidify solutions.
- NH_4^+ is the conjugate acid of NH_3
- Therefore, if NH_4NO_3 is added to water:



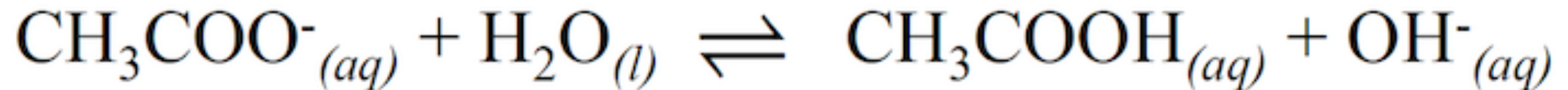
The pH drops below 7 because $[\text{H}_3\text{O}^+]$ increases.

Some Cations Acidify Solutions

- The ability to release protons from water increases as:
 - Ionic radius decreases
 - Charge increases (Fe^{3+} decreases the pH more than Fe^{2+})
 - Fe^{3+} is smaller with more net positive charge
- Conjugate acids of strong bases **will not** affect pH
 - Group 1A cations, Ca^{2+} , Sr^{2+} , and Ba^{2+}
 - Large radii and/or small net (+) charge

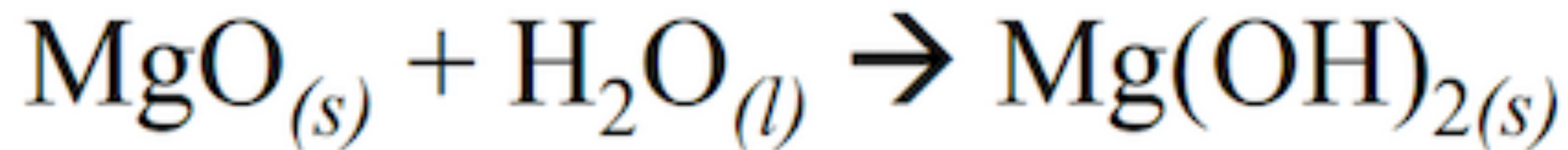
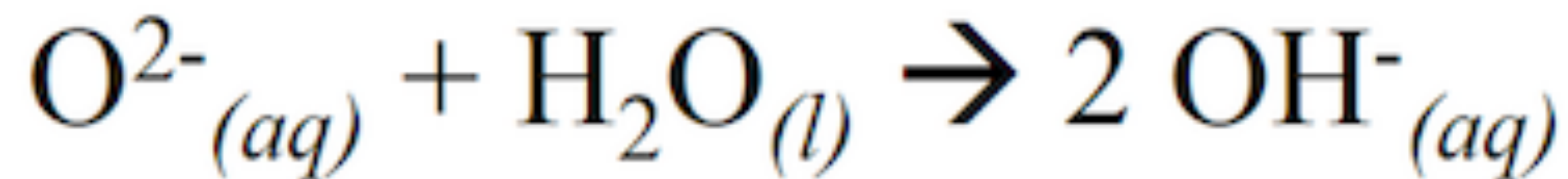
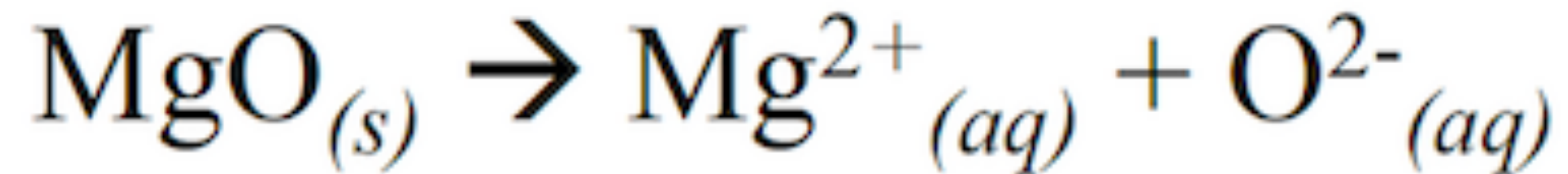
Some Anions Make Solutions Basic

- Anions that are conjugate bases of weak acids accept protons from water to produce OH⁻.
- The conjugate bases of strong acids will not raise the pH of a solution.
 - (Cl⁻, ClO₄⁻, I⁻, NO₃⁻, Br⁻, HSO₄⁻ do not accept protons from water)
- Example: NaCH₃CO₂ is added to water



Metal Oxides are Basic

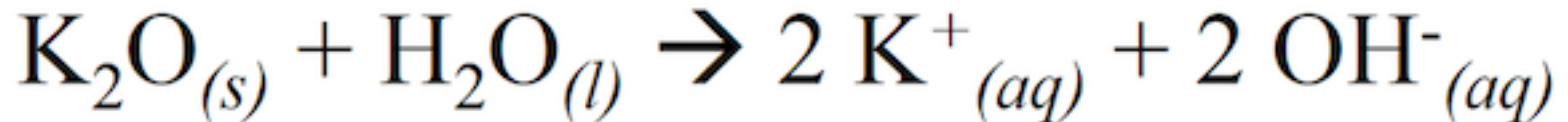
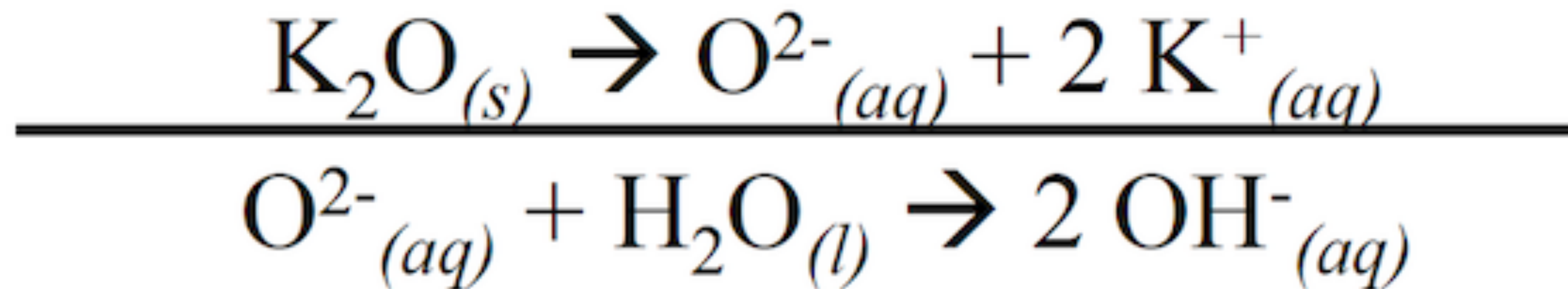
- Metal oxides can form solid hydroxides.



- The slight solubility of solid hydroxides increases $[\text{OH}^-]$ in the solution.

Example: Metal Oxides are Basic

- Write the net ionic equation for the reaction that takes place when solid potassium oxide is dropped into water.



Salts with Weak Acids & Weak Bases

- Some salts have an acidic cation and a basic anion.
- Solutions containing these salts tend to have **little or no overall affect on pH.**

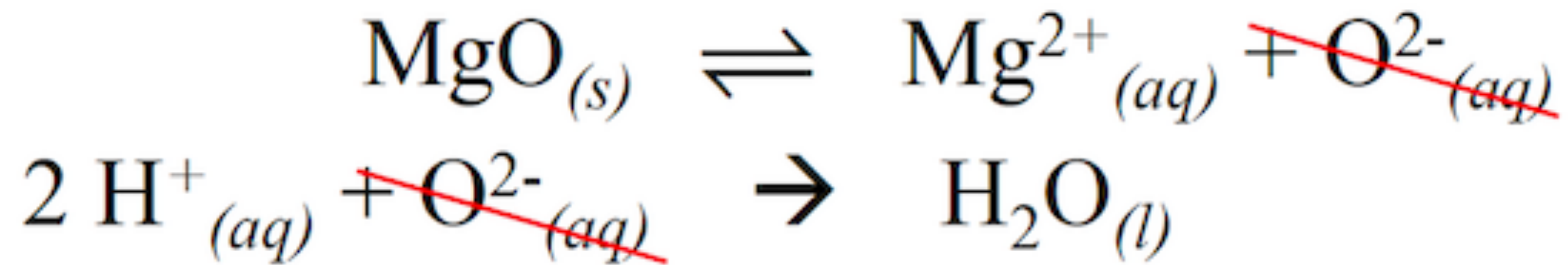


will donate H^+

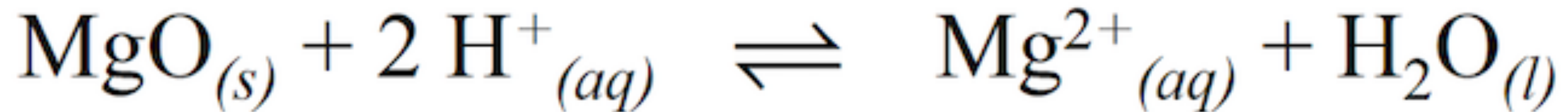
will accept H^+

Example: Slightly Soluble Ionic Compounds in Strong Acidic Solutions

- Solid magnesium oxide is added to a solution of nitric acid. Write the net ionic equation for the overall reaction.



Net Ionic Equation

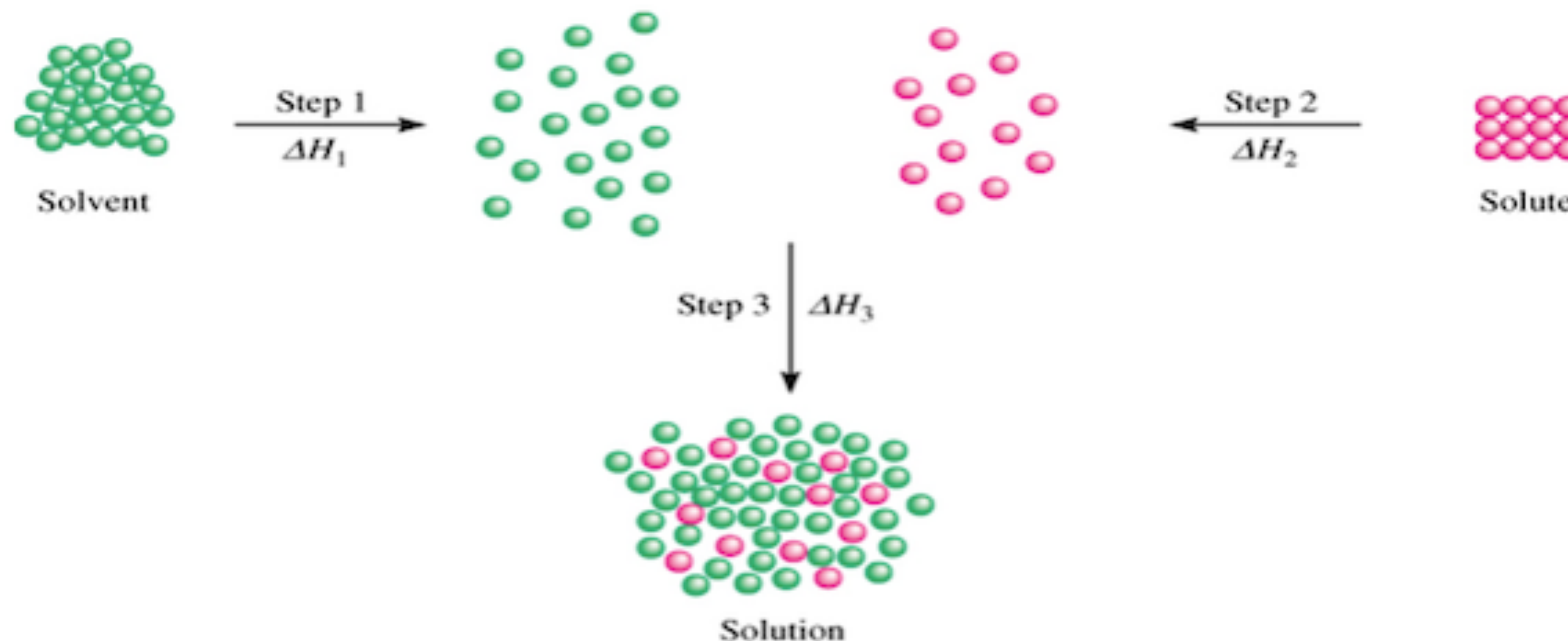


7.14 Spontaneity and Solubility

- Energy of Dissolution
- Temperature Implications

Spontaneous Processes

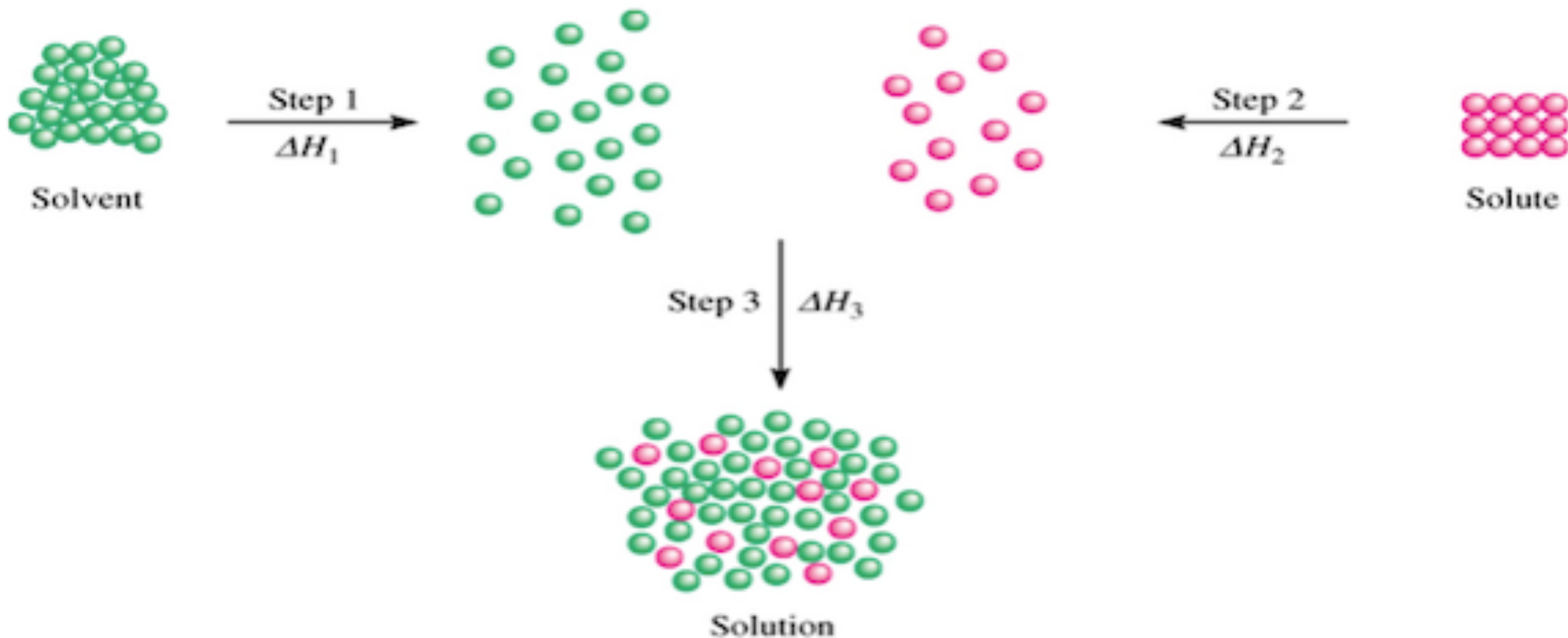
- When a reaction happens under a given set of circumstances, without any outside forces, it is said to be spontaneous.
- Doesn't have to be a FAST reaction, but it will just happen without any 'help'.
- Iron exposed to water and oxygen forms rust (FeO_2 and Fe_2O_3), but rust does not spontaneously change back to iron.



Free Energy of Dissolution

- Microstates - all of the tiny, individual places within a container that the particles can occupy.
- Dissolving a solid into a solution increases the amount of entropy (+ ΔS).

$$\Delta G = \Delta H - T\Delta S$$



Step	ΔH	ΔS
1 - Solvent separates (overcomes IMFs)	+	+
2 - Solute separates (overcomes IMFs)	+	+
3 - The solution forms (forming IMFs)	-	-